

[70240413 Statistical Machine Learning, Spring, 2015]

# Deep Learning

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# Why going deep?

- ◆ Data are often high-dimensional.
- ◆ There is a huge amount of **structure** in the data, but the structure is too complicated to be represented by a simple model.
- ◆ Insufficient depth can require more **computational elements** than architectures whose depth matches the task.
- ◆ Deep nets provide simpler but more descriptive models of many problems.

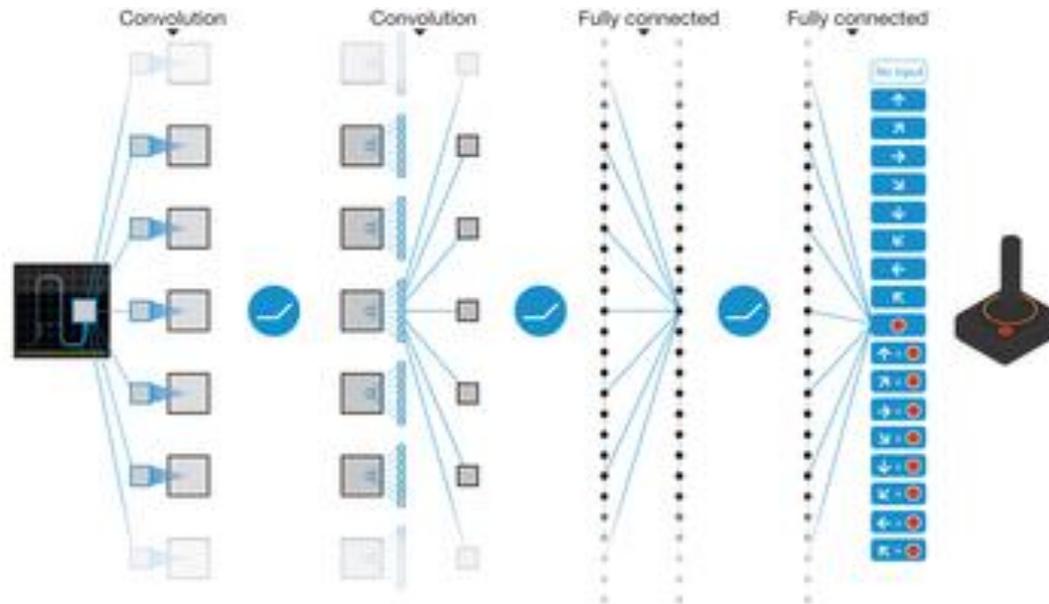
# Microsoft's speech recognition system

◆ [http://v.youku.com/v\\_show/id\\_XNDc0MDY4ODI0.html](http://v.youku.com/v_show/id_XNDc0MDY4ODI0.html)



# Human-Level Control via Deep RL

- ◆ Deep Q-network with human-level performance on A



- ◆ Minjie will talk more in next lecture



# MIT 10 Breakthrough Tech 2013

MIT Technology Review

## 10 BREAKTHROUGH TECHNOLOGIES 2013

Introduction   The 10 Technologies   Past Years

### Deep Learning

With massive amounts of computational power, machines can now recognize objects and translate speech in real time. Artificial intelligence is finally getting smart.

<http://www.technologyreview.com/featuredstory/513696/deep-learning/>

# Deep Learning in industry



Driverless car



Face identification



Speech recognition

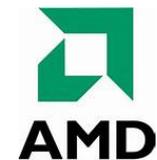


Web search

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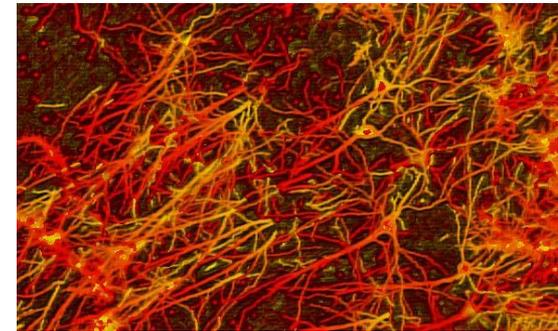
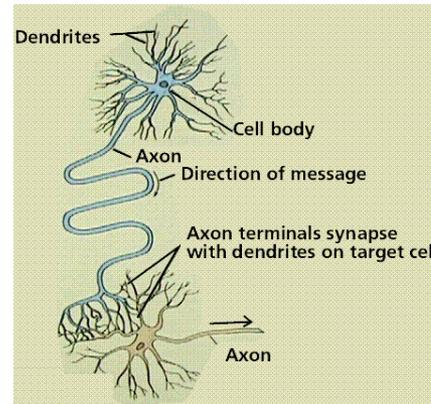
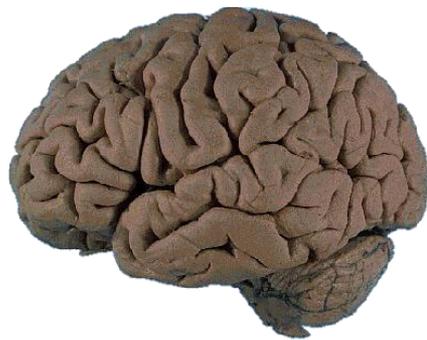




# Deep Learning Models



# How brains seem to do computing?



The business end of this is made of lots of these joined in networks like this

Much of our own “computations” are performed in/by this network

Learning occurs by changing the effectiveness of the synapses so that the influence of one neuron on another changes

# History of neural networks



Pitts



McCulloch



Rosenblatt



Minsky



Papert



Ackley

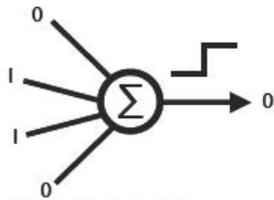


Hinton



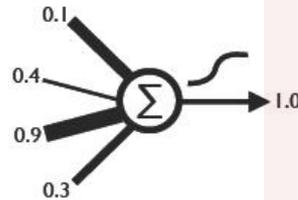
Sejnowski

1943



Artificial Neuron

1960



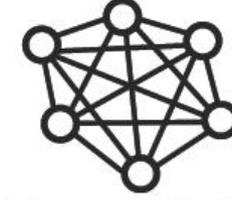
Perceptron

1969



Perceptrons

1985



Boltzmann Machine

# History of neural networks



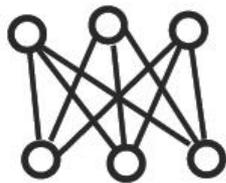
Smolensky



Hinton

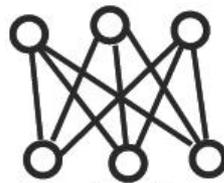
Hinton et al.

1986



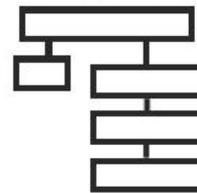
Harmoniums  
(Restricted Boltzmann Machine)

2002



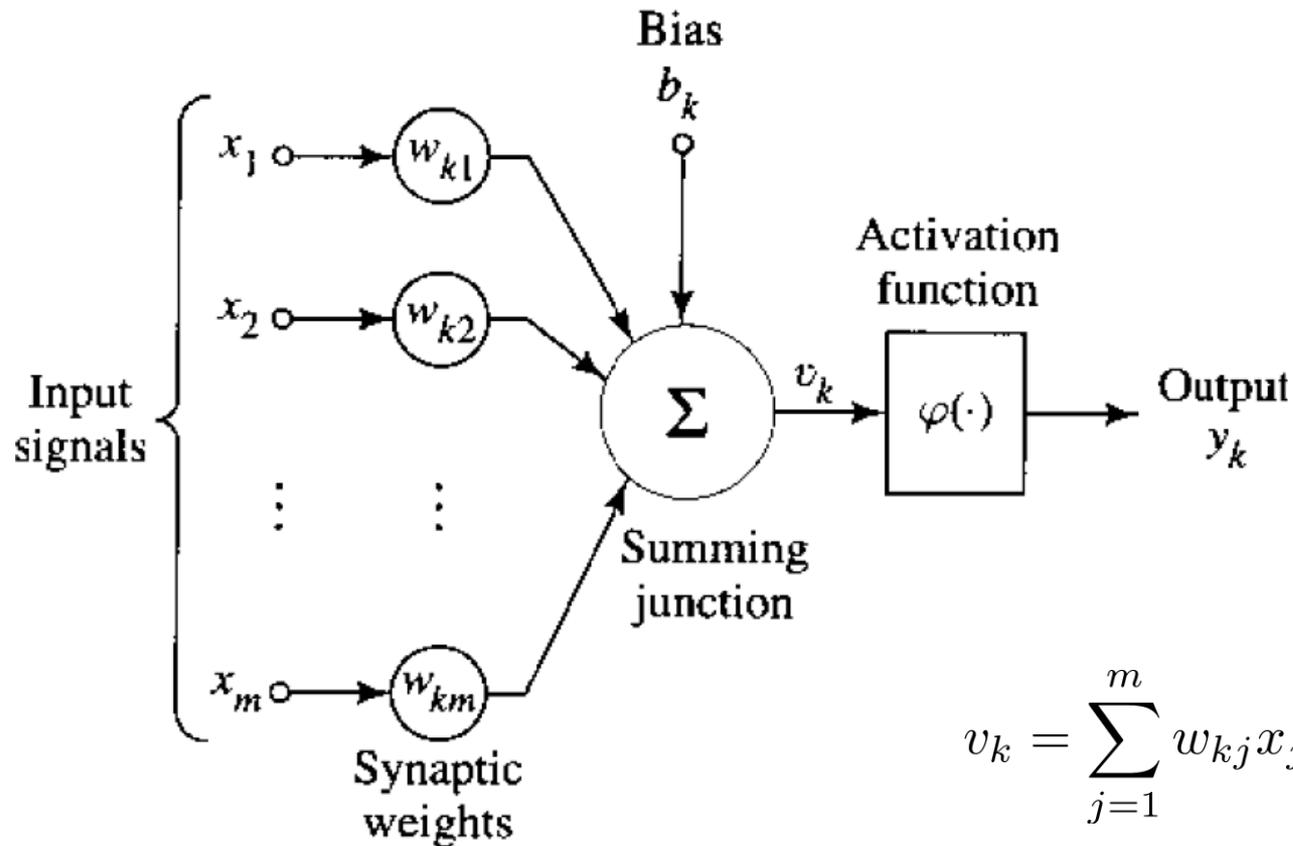
Contrastive  
Divergence

2006



Deep Belief  
Networks

# Model of a neuron

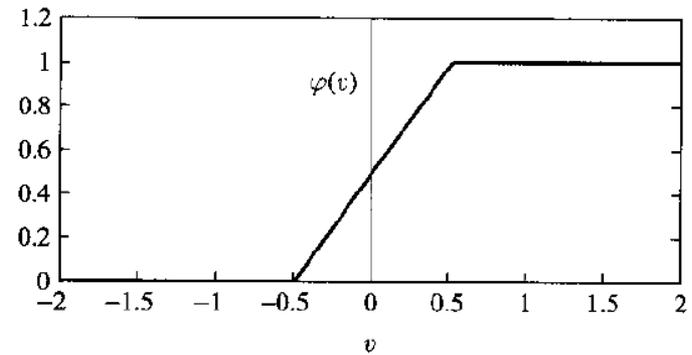
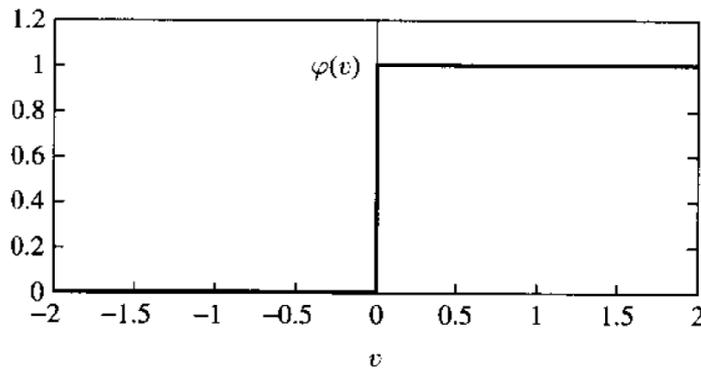


$$v_k = \sum_{j=1}^m w_{kj} x_j + b_k$$

$$y_k = \psi(v_k)$$

# Activation function

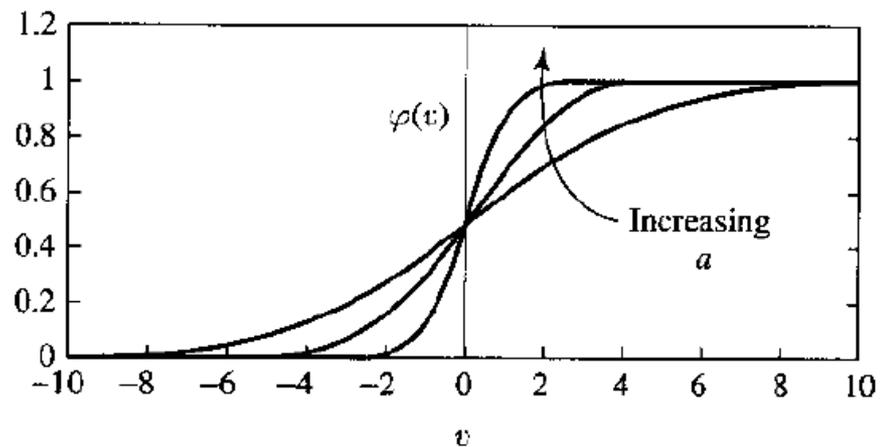
◆ Threshold function & piecewise linear function:



◆ Sigmoid function

$$\psi_a(v) = \frac{1}{1 + \exp(-av)}$$

$a \rightarrow \infty$  : step function



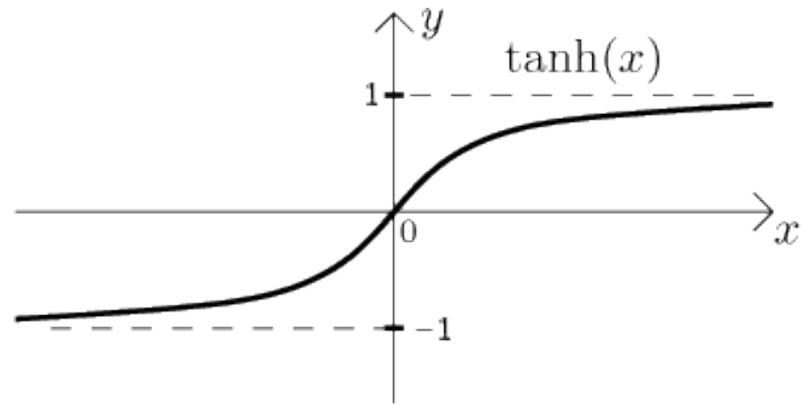
# Activation function with negative values

- ◆ Threshold function & piecewise linear function:

$$\text{sgn}(x) = \begin{cases} 1 & \text{if } x \geq 0 \\ -1 & \text{if } x < 0 \end{cases}$$

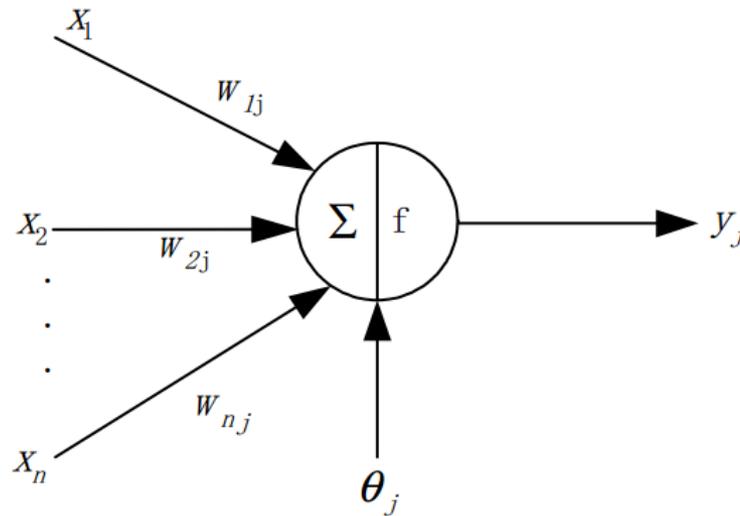
- ◆ Hyperbolic tangent function

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



# McCulloch & Pitts's Artificial Neuron

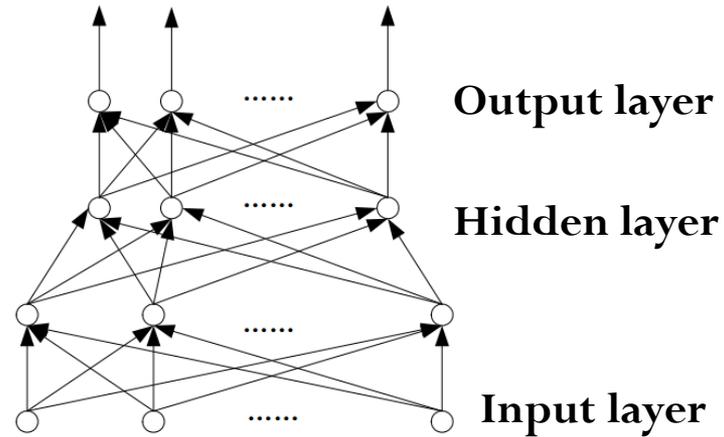
- ◆ The first model of artificial neurons in 1943
  - Activation function: a threshold function



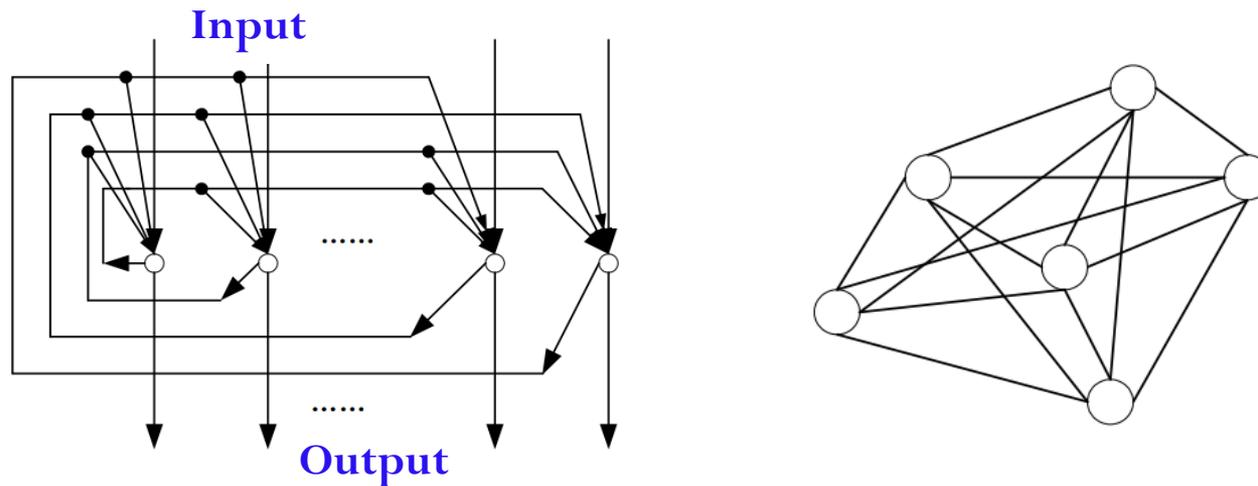
$$y_j = \text{sgn} \left( \sum_i w_{ij} x_i - \theta_j \right)$$

# Network Architecture

## ◆ Feedforward networks

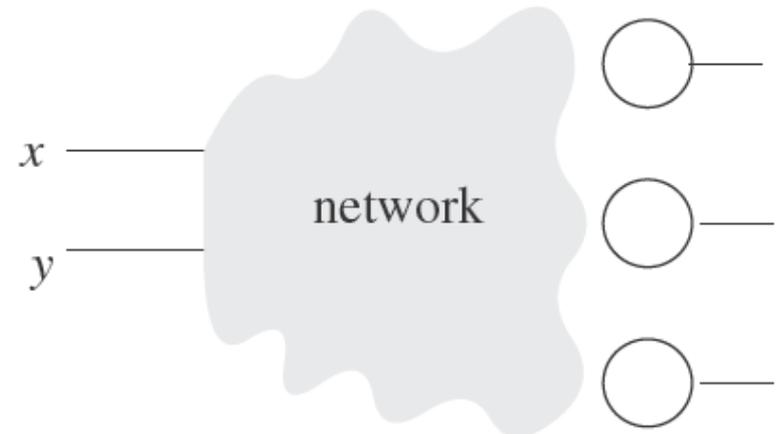
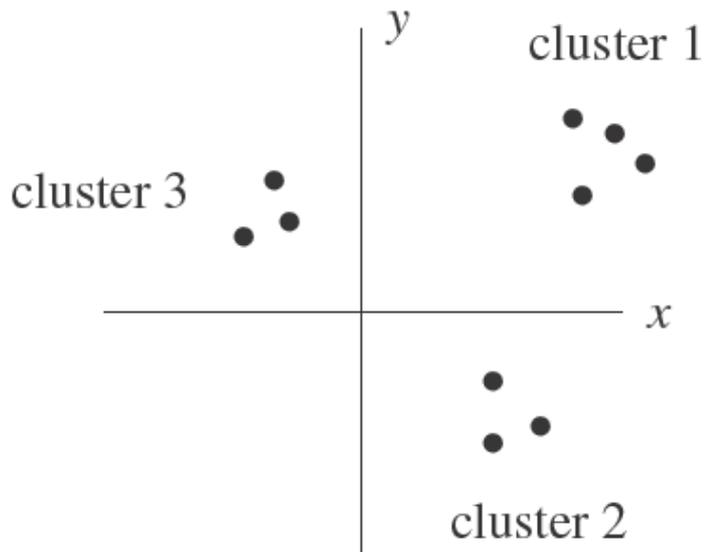


## ◆ Recurrent networks



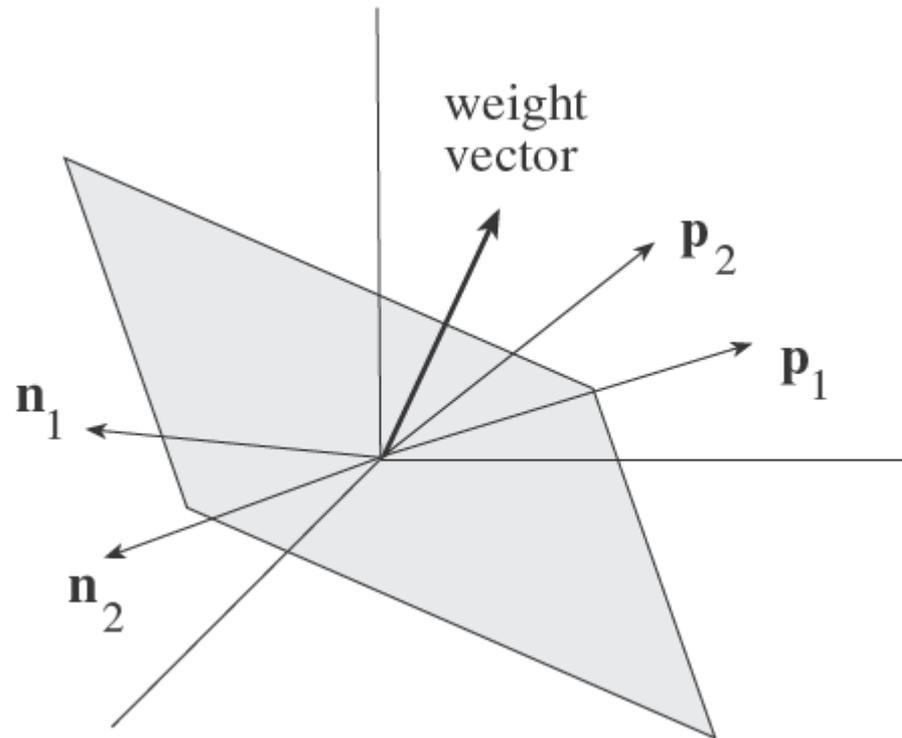
# Learning Paradigms

- ◆ Unsupervised learning (learning without a teacher)
  - Example: [clustering](#)



# Learning Paradigms

- ◆ Supervised Learning (learning with a teacher)
  - For example, classification: learns a separation plane



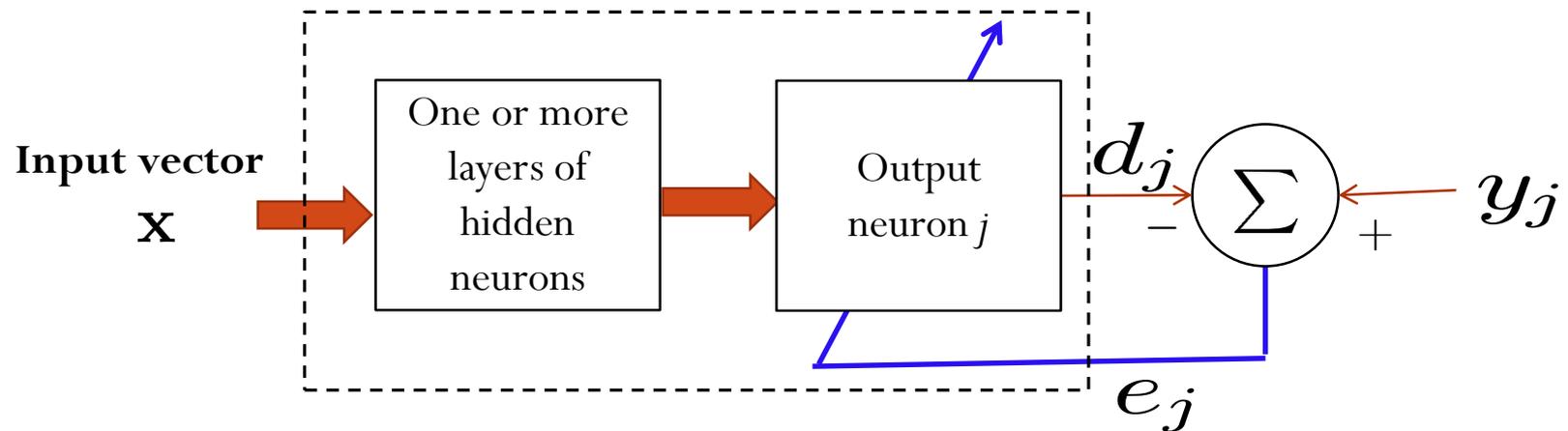


# Learning Rules

- ◆ Error-correction learning
- ◆ Competitive learning
- ◆ Hebbian learning
- ◆ Boltzmann learning
- ◆ Memory-base learning
  - Nearest neighbor, radial-basis function network

# Error-correction learning

- ◆ The generic paradigm:



- Error signal:

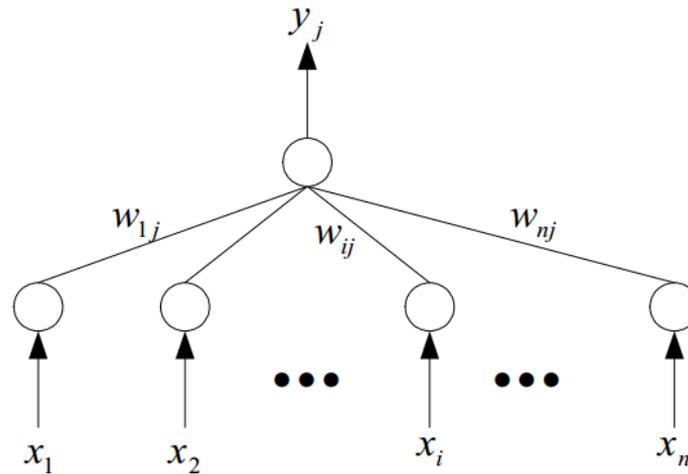
$$e_j = y_j - d_j$$

- Learning objective:

$$\min_{\mathbf{w}} R(\mathbf{w}; \mathbf{x}) := \frac{1}{2} \sum_j e_j^2$$

## Example: Perceptron

- ◆ One-layer feedforward network based on error-correction learning (no hidden layer):



- Current output (at iteration  $t$ ):

$$d_j = (\mathbf{w}_t^j)^\top \mathbf{x}$$

- Update rule (*exercise?*):

$$\mathbf{w}_{t+1}^j = \mathbf{w}_t^j + \eta(y_j - d_j)\mathbf{x}$$

# Perceptron for classification

◆ Consider a single output neuron

◆ Binary labels:

$$y \in \{+1, -1\}$$

◆ Output function:

$$d = \text{sgn} \left( \mathbf{w}_t^\top \mathbf{x} \right)$$

◆ Apply the error-correction learning rule, we get ... (next slide)

# Perceptron for Classification

◆ Set  $\mathbf{w}_1 = 0$  and  $t=1$ ; scale all examples to have length 1 (doesn't affect which side of the plane they are on)

◆ Given example  $\mathbf{x}$ , predict positive *iff*

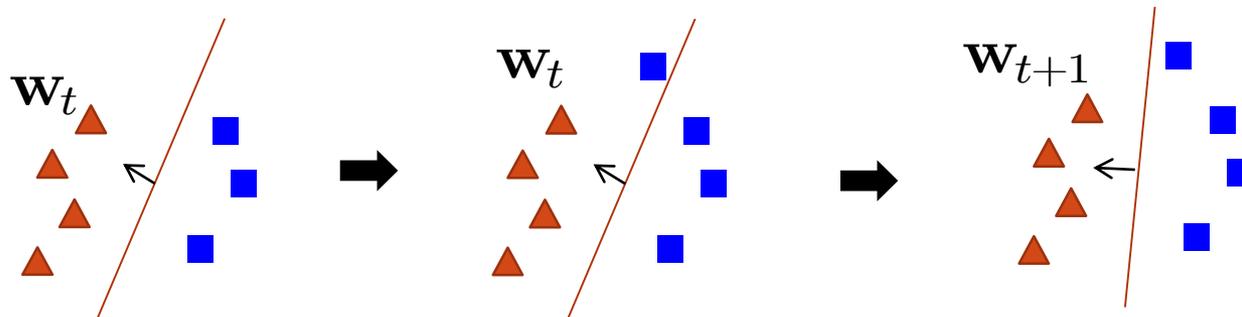
$$\mathbf{w}_t^\top \mathbf{x} > 0$$

◆ If a mistake, update as follows

□ Mistake on positive:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + \eta_t \mathbf{x}$

□ Mistake on negative:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t - \eta_t \mathbf{x}$

$t \leftarrow t + 1$





# Convergence Theorem

- ◆ For linearly separable case, the perceptron algorithm will converge in a finite number of steps

# Mistake Bound

## ◆ Theorem:

- Let  $\mathcal{S}$  be a sequence of labeled examples consistent with a linear threshold function  $\mathbf{w}_*^\top \mathbf{x} > 0$ , where  $\mathbf{w}_*$  is a unit-length vector.
- The number of mistakes made by the online Perceptron algorithm is at most  $(1/\gamma)^2$ , where

$$\gamma = \min_{\mathbf{x} \in \mathcal{S}} \frac{|\mathbf{w}_*^\top \mathbf{x}|}{\|\mathbf{x}\|}$$

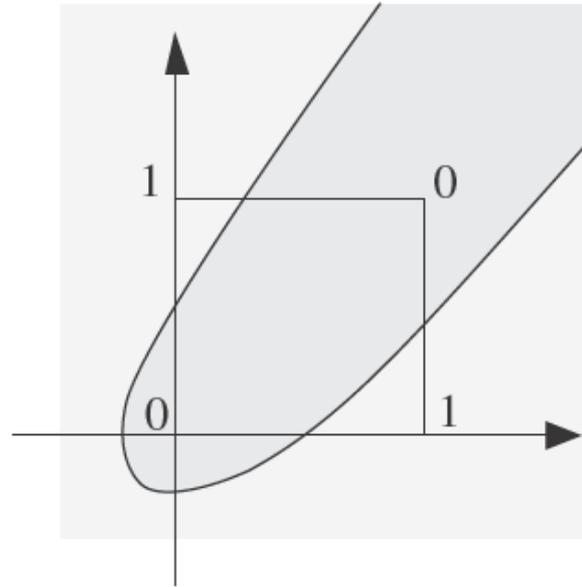
- i.e.: if we scale examples to have length 1, then  $\gamma$  is the minimum distance of any example to the plane  $\mathbf{w}_*^\top \mathbf{x} = 0$
- $\gamma$  is often called the “margin” of  $\mathbf{w}_*$ ; the quantity  $\frac{\mathbf{w}_*^\top \mathbf{x}}{\|\mathbf{x}\|}$  is the cosine of the angle between  $\mathbf{x}$  and  $\mathbf{w}_*$



# Deep Nets

- ◆ Multi-layer Perceptron
- ◆ CNN
- ◆ Auto-encoder
- ◆ RBM
- ◆ Deep belief nets
- ◆ Deep recurrent nets

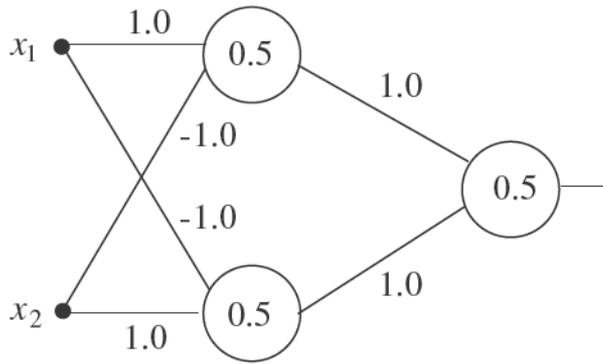
# XOR Problem



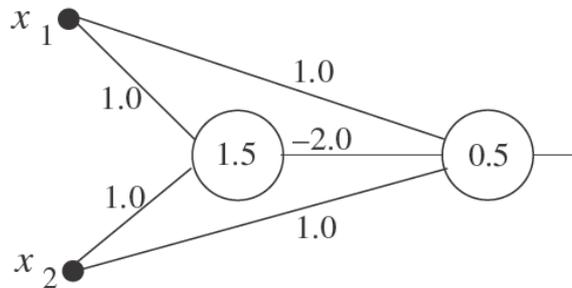
◆ Single-layer perceptron can't solve the problem

# XOR Problem

- ◆ A network with 1-layer of 2 neurons works for XOR:
  - ▣ threshold activation function



- ▣ Many alternative networks exist (not layered)



# Multilayer Perceptrons

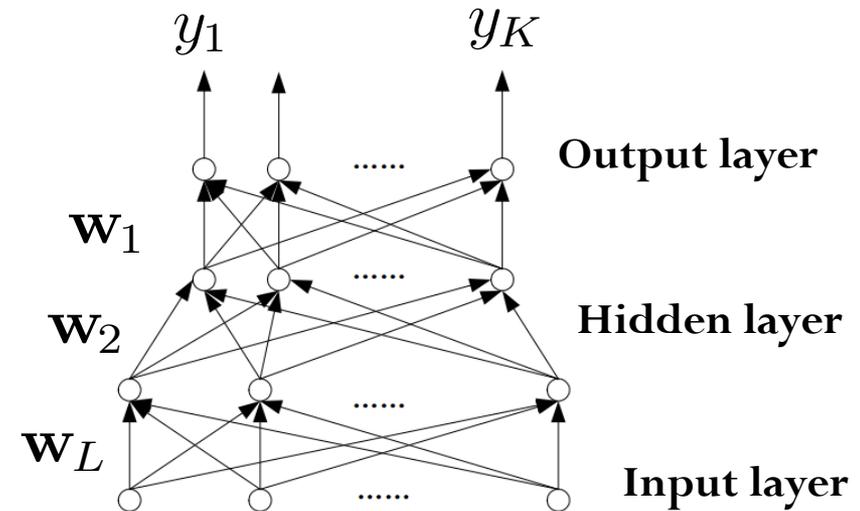
- ◆ Computational limitations of single-layer Perceptron by Minsky & Papert (1969)
- ◆ Multilayer Perceptrons:
  - Multilayer feedforward networks with an error-correction learning algorithm, known as error *back-propagation*
  - A generalization of single-layer perceptron to allow nonlinearity

# Backpropagation

- ◆ Learning as loss minimization

$$\mathbf{w}^* = \arg \min_{\mathbf{w}} \frac{1}{2} \sum_j e_j^2(\mathbf{x})$$

$$e_j = y_j - d_j$$



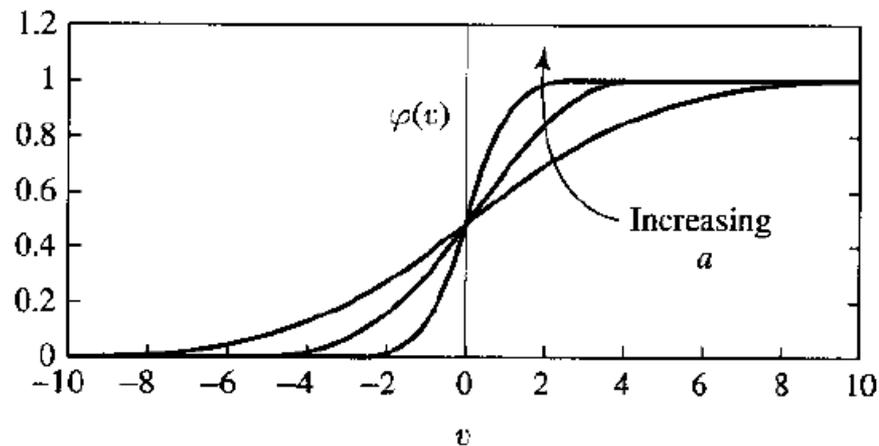
- ◆ Learning with gradient descent

$$\mathbf{w}_{t+1} = \mathbf{w}_t - \lambda_t \nabla R(\mathbf{w}; \mathcal{D})$$

# Backpropagation

- ◆ Step function in perceptrons is non-differentiable
- ◆ Differentiable activation functions are needed to calculate gradients, e.g., sigmoid:

$$\psi_{\alpha}(v) = \frac{1}{1 + \exp(-\alpha v)}$$



# Backpropagation

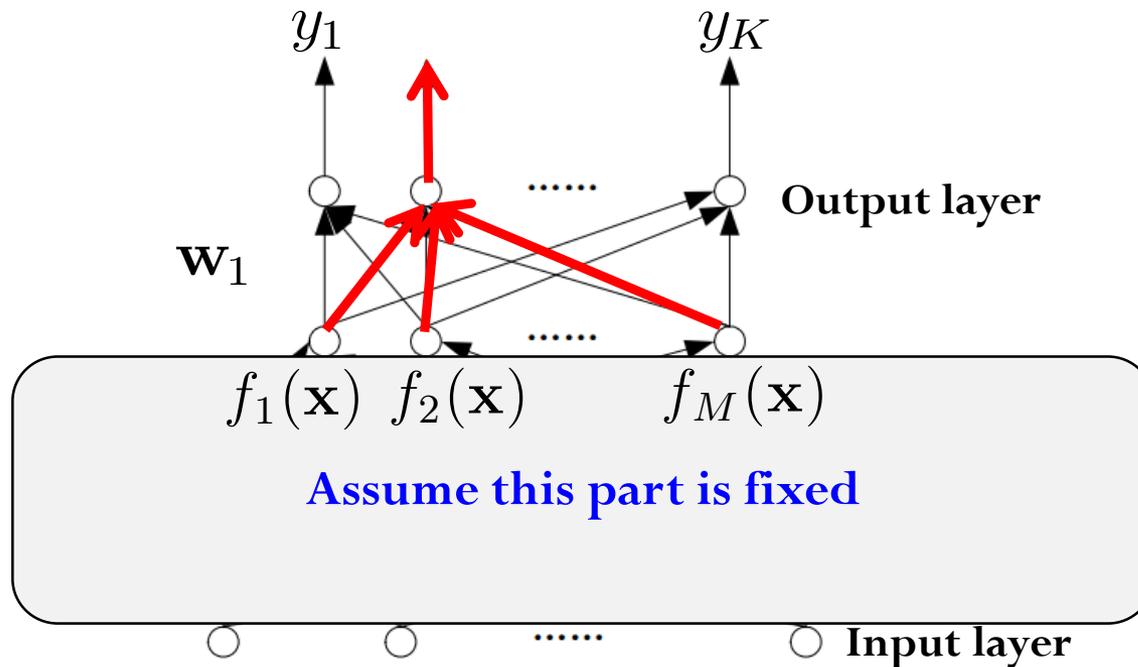
- ◆ Derivative of a sigmoid function ( $\alpha = 1$ )

$$\nabla_v \psi(v) = \frac{e^{-v}}{(1 + e^{-v})^2} = \psi(v)(1 - \psi(v))$$

- Notice about the small scale of the gradient
  - Gradient vanishing issue
- 
- ◆ Many other activation functions examined

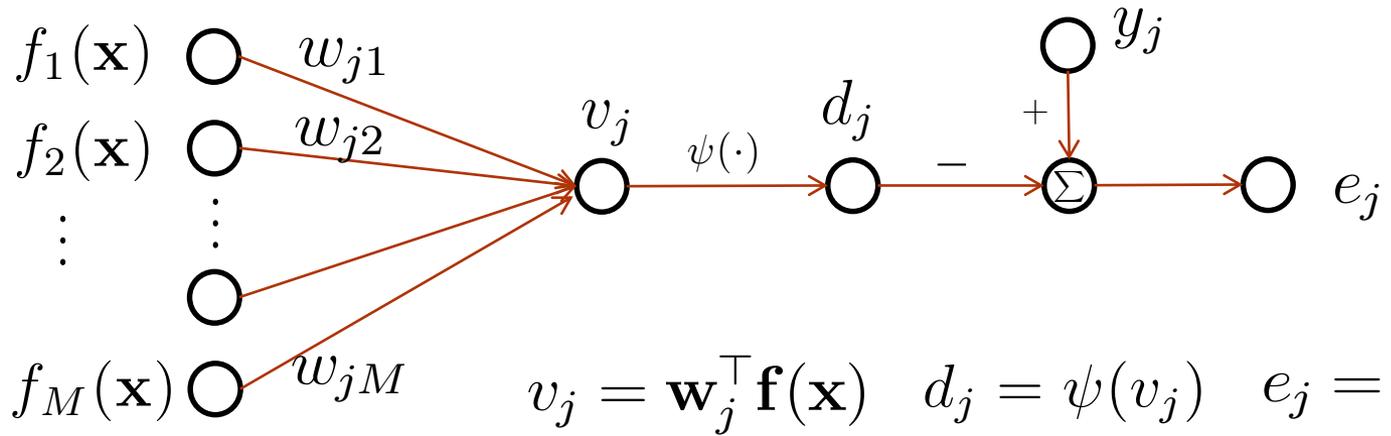
# Gradient computation at output layer

- ◆ Output neurons are separate:



# Gradient computation at output layer

◆ Signal flow:



$$R_j = \frac{1}{2} e_j^2$$

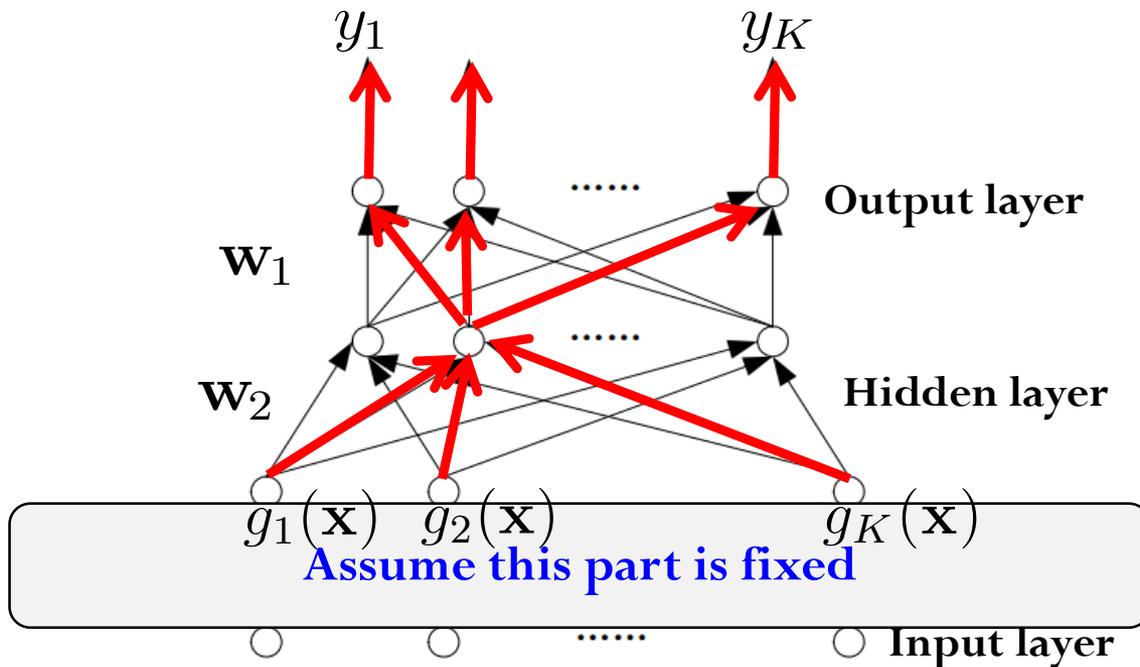
$$R = \frac{1}{2} \sum_j e_j^2$$

$$\begin{aligned}
 \nabla_{w_{ji}} R &= \frac{\partial R_j}{\partial e_j} \frac{\partial e_j}{\partial d_j} \frac{\partial d_j}{\partial v_j} \frac{\partial v_j}{\partial w_{ji}} \\
 &= e_j \cdot (-1) \cdot \psi'(v_j) \cdot f_i(\mathbf{x}) \\
 &= -e_j \psi'(v_j) f_i(\mathbf{x})
 \end{aligned}$$

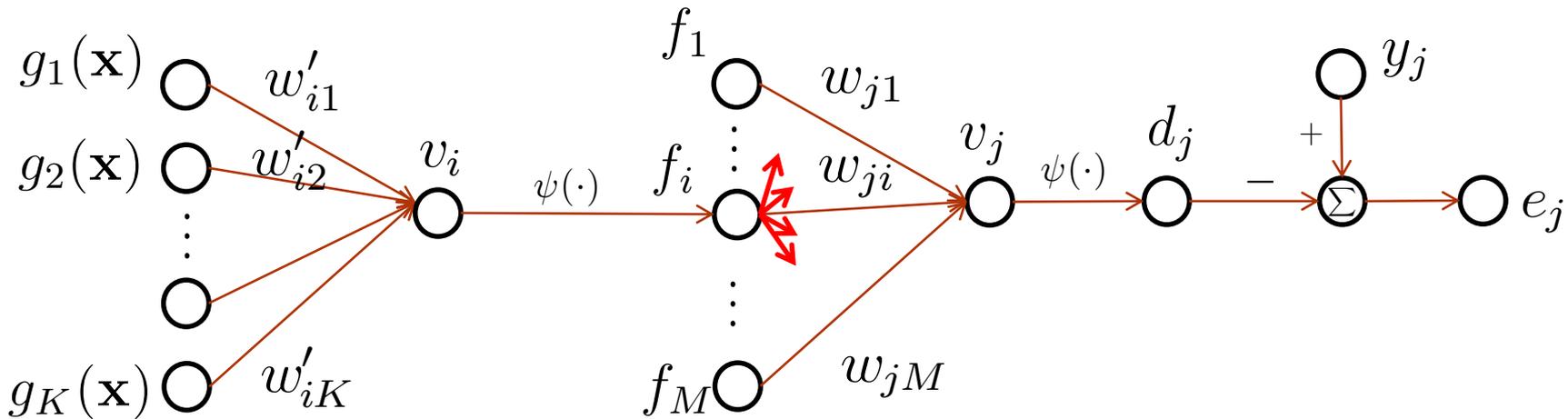
Local gradient:  $\delta_j = -\frac{\partial R}{\partial v_j}$

# Gradient computation at hidden layer

- ◆ Output neurons are NOT separate:



# Gradient computation at hidden layer



$$v_i = (\mathbf{w}'_i)^\top \mathbf{g} \quad f_i = \psi(v_i) \quad v_j = \mathbf{w}_j^\top \mathbf{f} \quad d_j = \psi(v_j) \quad e_j = y_j - d_j$$

$$R_j = \frac{1}{2} e_j^2$$

$$R = \frac{1}{2} \sum_j e_j^2$$

$$\nabla_{w'_{ik}} R = \sum_j \frac{\partial R_j}{\partial e_j} \frac{\partial e_j}{\partial d_j} \frac{\partial d_j}{\partial v_j} \frac{\partial v_j}{\partial f_i} \frac{\partial f_i}{\partial v_i} \frac{\partial v_i}{\partial w'_{ik}}$$

$$= - \sum_j e_j \psi'(v_j) w_{ji} \psi'(v_i) g_k(\mathbf{x})$$

$$= - \sum_j \delta_j w_{ji} \psi'(v_i) g_k(\mathbf{x})$$

Local gradient:  $\delta_i = - \frac{\partial R}{\partial v_i}$

# Back-propagation formula

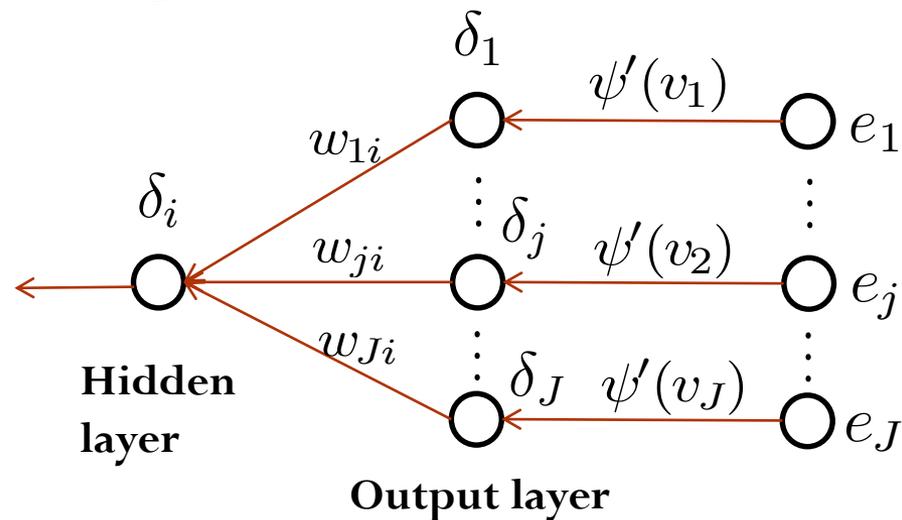
◆ The update rule of **local gradients**:

▣ for hidden neuron  $i$ :

$$\delta_i = \psi'(v_i) \sum_j \delta_j w_{ji}$$


Only depends on the activation function at hidden neuron  $i$

◆ Flow of error signal:



# Back-propagation formula

◆ The update rule of weights:

□ Output neuron:

$$\Delta w_{ji} = \lambda \cdot \delta_j \cdot f_i(\mathbf{x})$$

□ Hidden neuron:

$$\Delta w'_{ik} = \lambda \cdot \delta_i \cdot g_k(\mathbf{x})$$

$$\begin{pmatrix} \textit{Weight} \\ \textit{correction} \\ \Delta w_{ji} \end{pmatrix} = \begin{pmatrix} \textit{learning} \\ \textit{rate} \\ \lambda \end{pmatrix} \cdot \begin{pmatrix} \textit{local} \\ \textit{gradient} \\ \delta_j \end{pmatrix} \cdot \begin{pmatrix} \textit{input signal} \\ \textit{of neuron } j \\ v_i \end{pmatrix}$$

# Two Passes of Computation

## ◆ Forward pass

- Weights fixed
- Start at the first hidden layer
- Compute the output of each neuron
- End at output layer

## ◆ Backward pass

- Start at the output layer
- Pass error signal backward through the network
- Compute local gradients

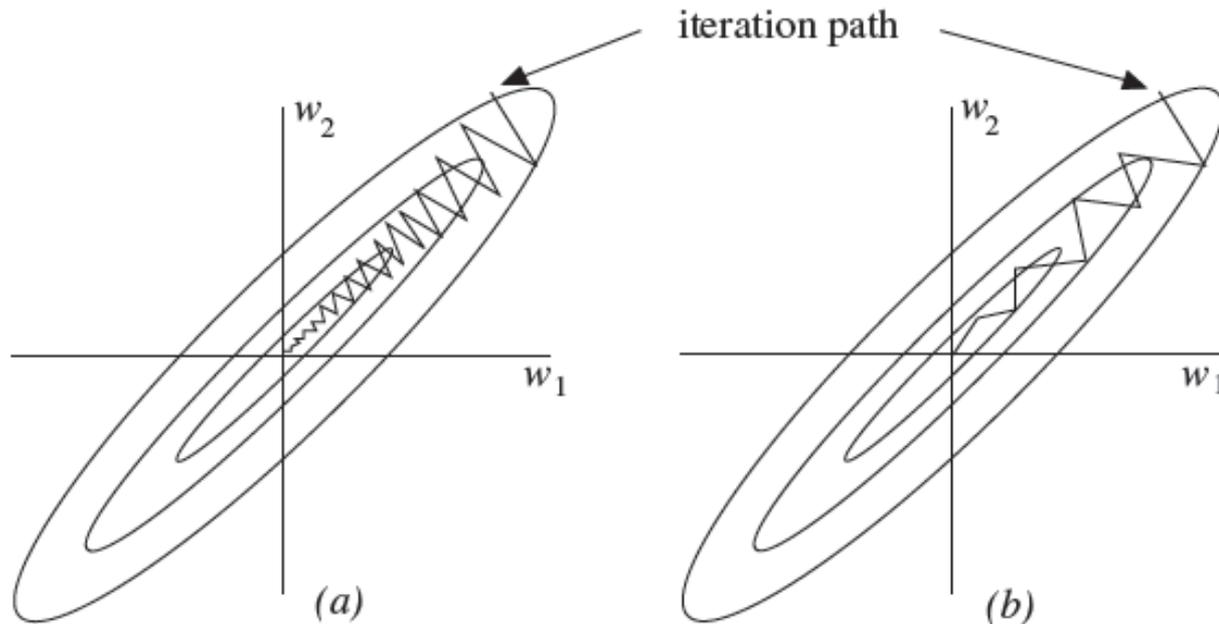
# Stopping Criterion

- ◆ No general rules
  
- ◆ Some reasonable heuristics:
  - The norm of gradient is small enough
  - The number of iterations is larger than a threshold
  - The training error is stable
  - ...

# Improve Backpropagation

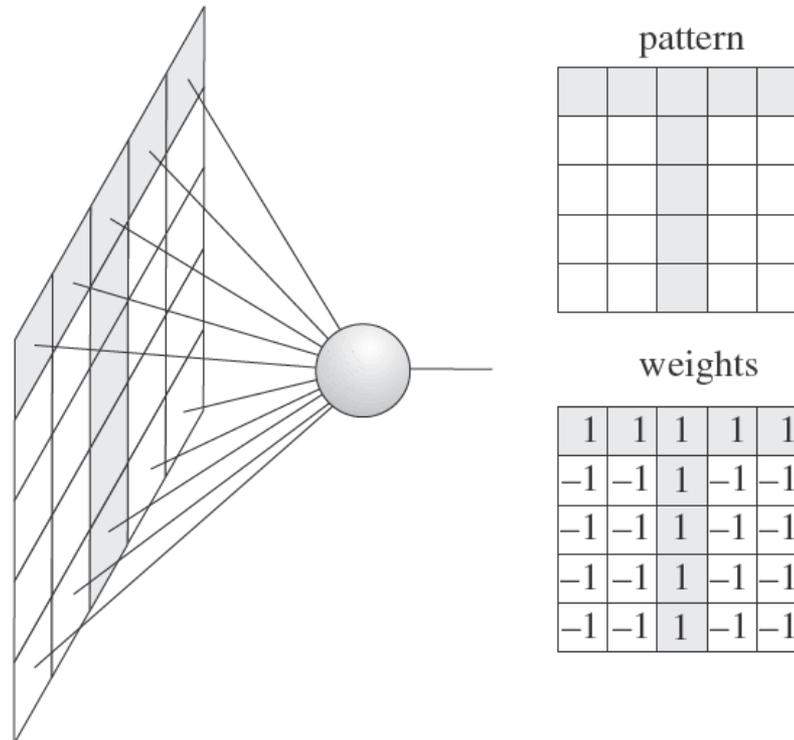
- ◆ Many methods exist to improve backpropagation
- ◆ E.g., backpropagation with momentum

$$\Delta w_{ij}^t = -\lambda \frac{\partial R}{\partial w_{ij}} + \alpha \Delta w_{ij}^{t-1}$$



# Neurons as Feature Extractor

- ◆ Compute the similarity of a pattern to the ideal pattern of a neuron
- ◆ Threshold is the minimal similarity required for a pattern
- ◆ Reversely, it visualizes the connections of a neuron

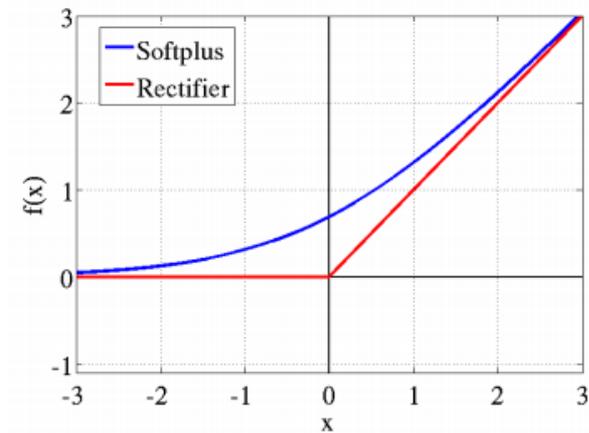
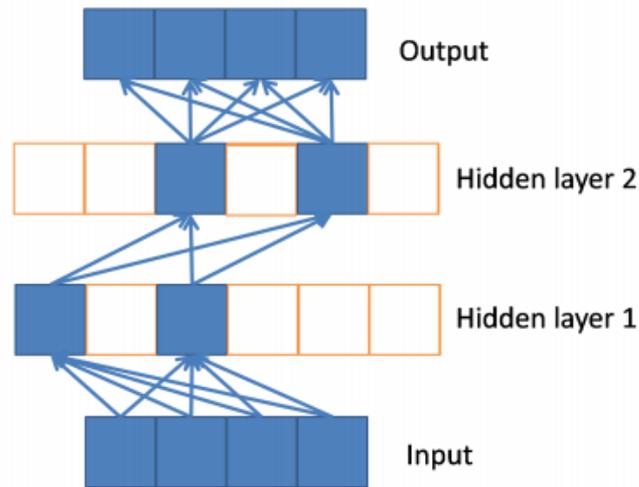


# Vanishing gradient problem

- ◆ The gradient can decrease exponentially during back-prop
- ◆ Solutions:
  - Pre-training + fine tuning
  - Rectifier neurons (sparse gradients)
- ◆ Ref:
  - Gradient flow in recurrent nets: the difficulty of learning long-term dependencies. Hochreiter, Bengio, & Frasconi, 2001

# Deep Rectifier Nets

- ◆ Sparse representations without gradient vanishing



- Non-linearity comes from the path selection
  - Only a subset of neurons are active for a given input
- Can be seen as a model with an exponential number of linear models that share weights

[Deep sparse rectifier neural networks. Glorot, Bordes, & Bengio, 2011]

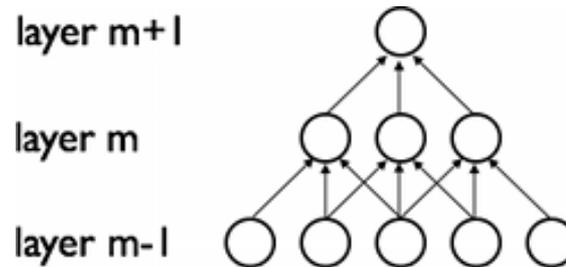


# CNN

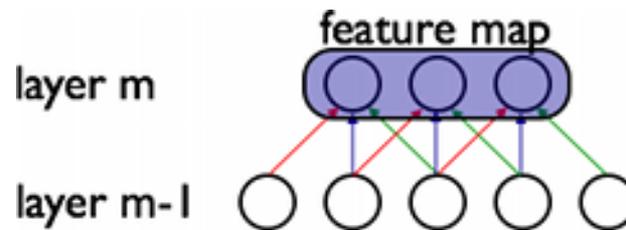
- ◆ Hubel and Wiesel's study on animal's visual cortex:
  - Cells that are sensitive to small sub-regions of the visual field, called a *receptive field*
  - Simple cells respond maximally to specific edge-like patterns within their receptive field. Complex cells have larger receptive fields and are locally invariant to the exact position of the pattern.

# Convolutional Neural Networks

- ◆ Sparse local connections (spatially contiguous receptive fields)

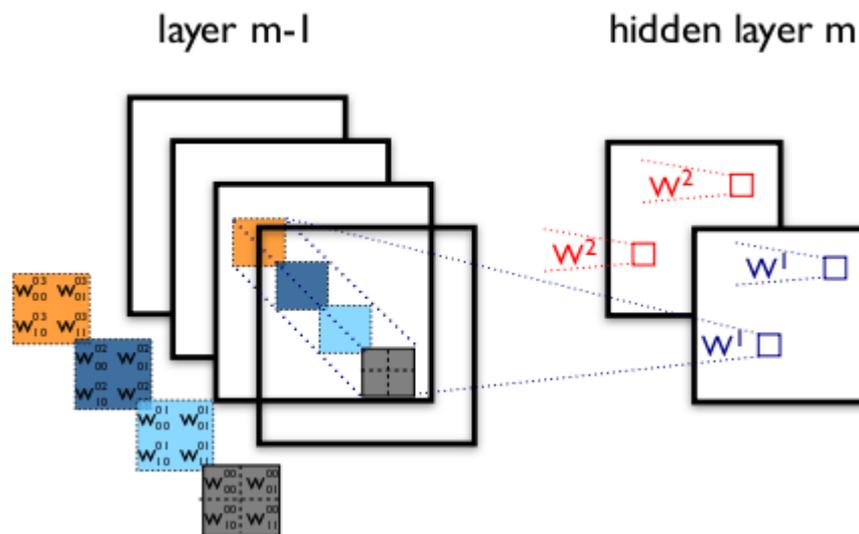


- ◆ Shared weights: each filter is replicated across the entire visual field, forming a feature map



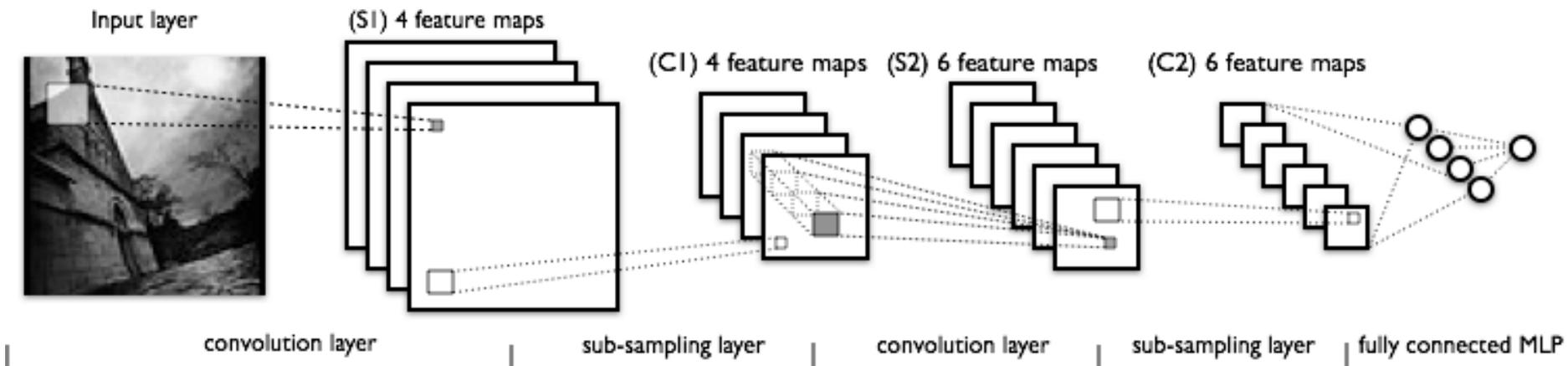
# CNN

- ◆ Each layer has multiple feature maps



# CNN

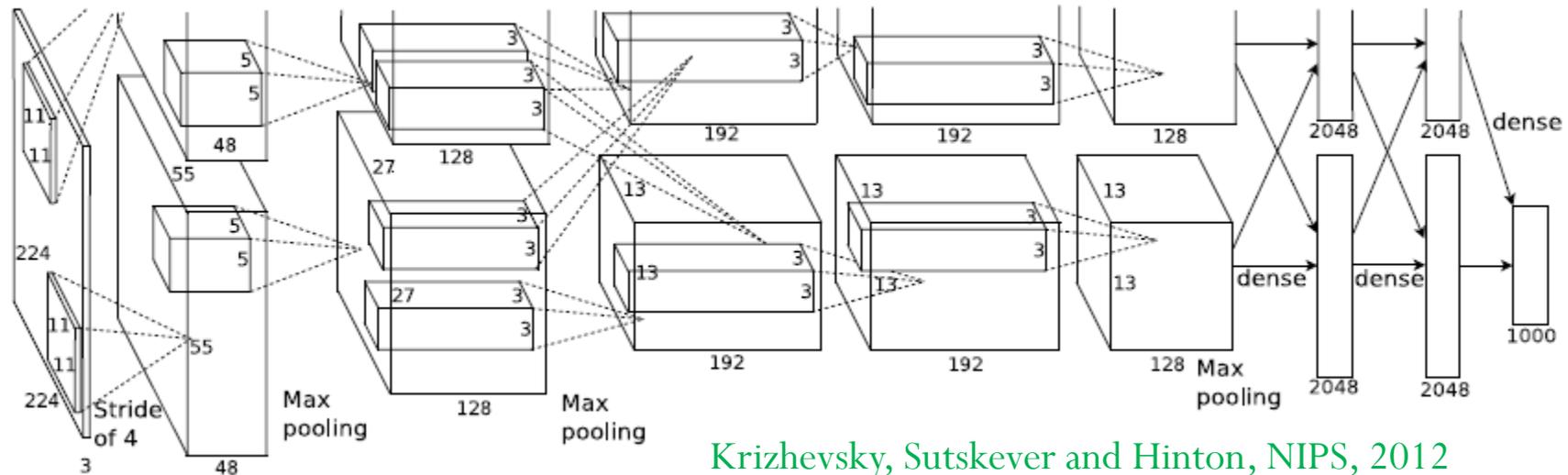
## ◆ The full model



## ◆ *Max-pooling*, a form of non-linear down-sampling.

- Max-pooling partitions the input image into a set of non-overlapping rectangles and, for each such sub-region, outputs the maximum value.

# Example: CNN for image classification



- ◆ Network dimension: 150,528(input)-253,440-186,624-64,896-64,896-43,264-4096-4096-1000(output)
  - In total: 60 million parameters
  - Task: classify 1.2 million high-resolution images in the ImageNet LSVRC-2010 contest into the 1000 different classes
  - Results: state-of-the-art accuracy on ImageNet

# Issues with CNN

- ◆ Computing the activations of a single convolutional filter is much more expensive than with traditional MLPs
  
- ◆ Many tuning parameters
  - # of filters:
    - Model complexity issue (overfitting vs underfitting)
  - Filter shape:
    - the right level of “granularity” in order to create abstractions at the proper scale, given a particular dataset
    - Usually 5x5 for MNIST at 1<sup>st</sup> layer
  - Max-pooling shape:
    - typical: 2x2; maybe 4x4 for large images

# Auto-Encoder

- ◆ Encoder: (a distributed code)

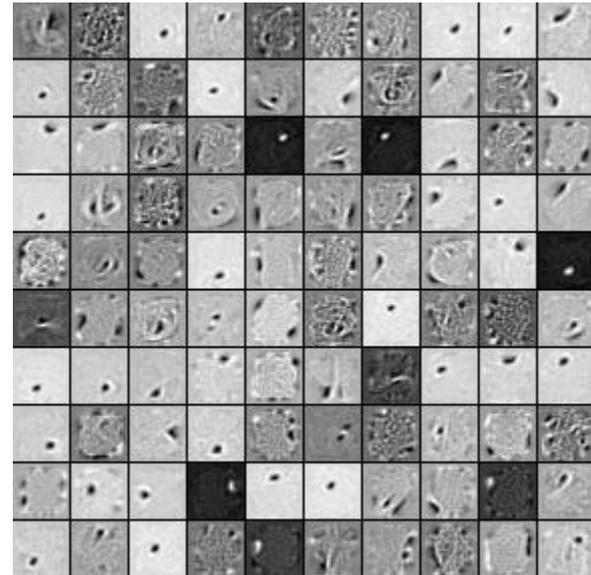
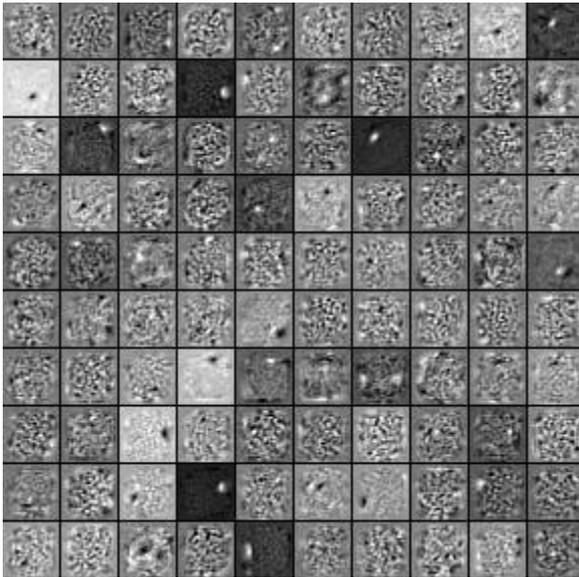
$$\mathbf{y} = s(\mathbf{W}\mathbf{x} + \mathbf{b})$$

- ◆ Decoder:

$$\mathbf{z} = s(\mathbf{W}'\mathbf{y} + \mathbf{b}')$$

- ◆ Minimize reconstruction error
- ◆ Connection to PCA
  - PCA is linear projection, which Auto-Encoder is nonlinear
  - Stacking PCA with nonlinear processing may perform as well (Ma Yi's work)
- ◆ Denoising Auto-Encoder
  - A stochastic version with corrupted noise to discover more robust features
  - E.g., randomly set some inputs to zero

◆ Left: no noise; right: 30 percent noise

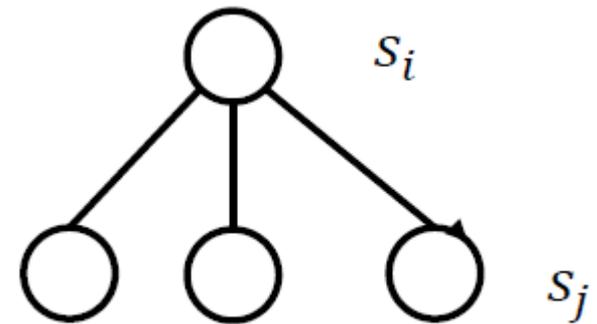
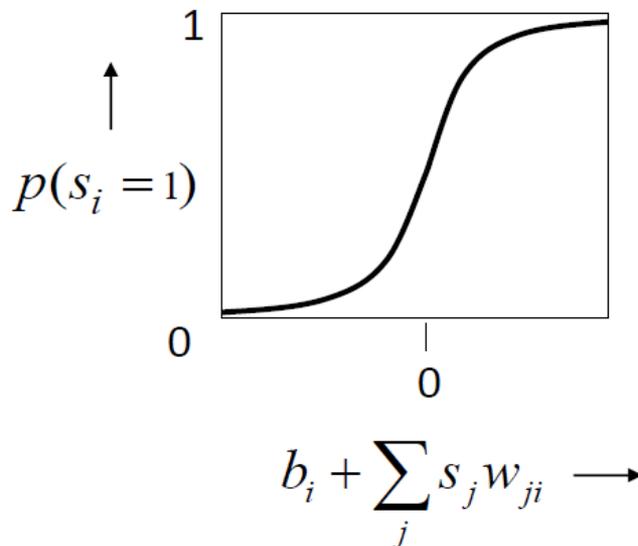


# Deep Generative Models

# Stochastic Binary Units

- ◆ Each unit has a state of 0 or 1
- ◆ The probability of turning on is determined by

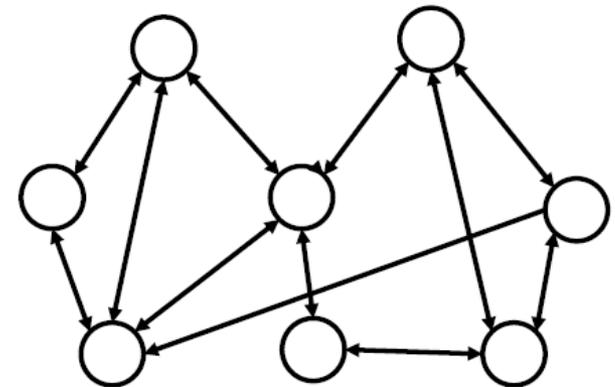
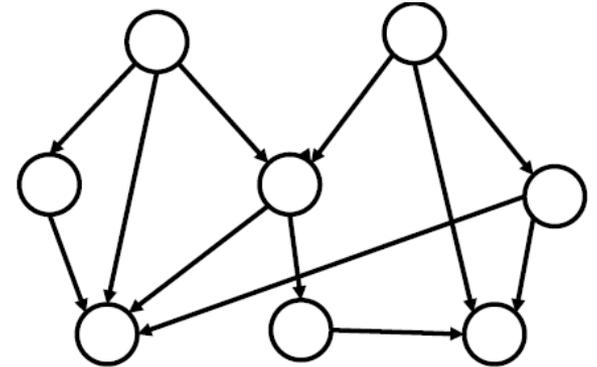
$$p(s_i = 1) = \frac{1}{1 + \exp(-b_i - \sum_j s_j w_{ji})}$$





# Generative Models

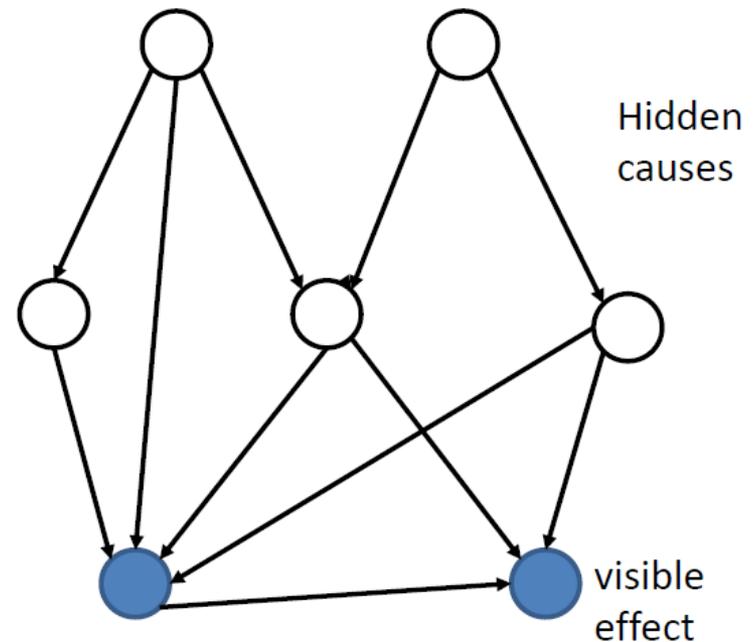
- ◆ Directed acyclic graph with stochastic binary units is termed Sigmoid Belief Net (Radford Neal, 1992)
- ◆ Undirected graph with stochastic binary units is termed Boltzmann Machine (Hinton & Sejnowski, 1983)





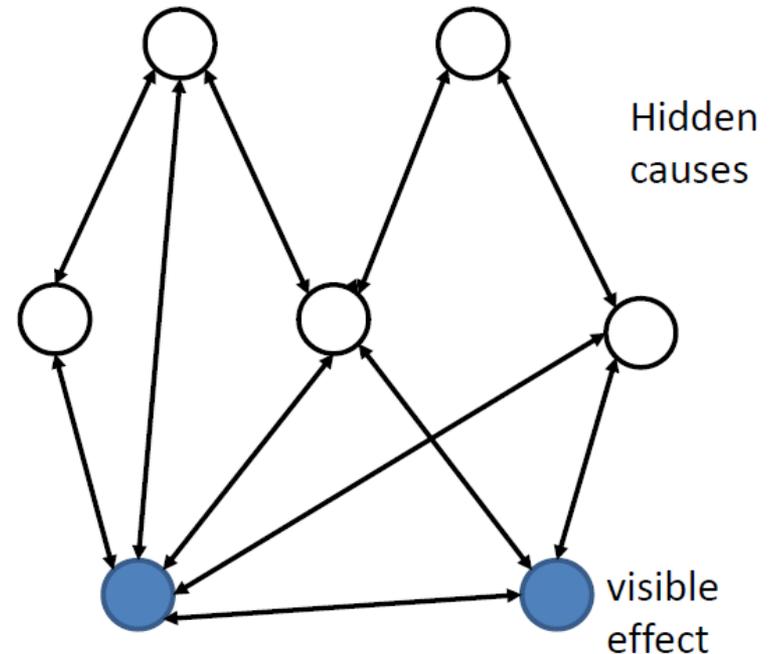
# Learning Deep Belief Nets

- ◆ **Easy to generate** an unbiased example at the leaf nodes
- ◆ **Hard to infer** the posterior distribution over all possible configurations of hidden causes – explain away effect!
  - Hard to even get a sample from the posterior



# Learning Boltzmann Machine

- ◆ Hard to generate an unbiased example for the visible units
- ◆ Hard to infer the posterior distribution over all possible configurations of hidden causes
- ◆ Hard to even get a sample from the posterior



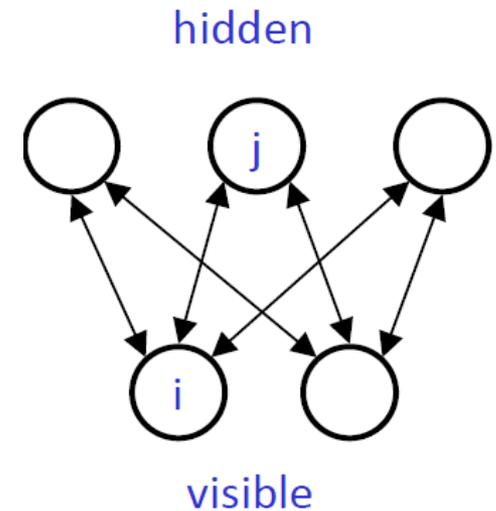
# Restricted Boltzmann Machines

- ◆ An energy-based model with hidden units

$$P(\mathbf{x}) = \sum_h P(\mathbf{x}, h) = \sum_h \frac{e^{-E(\mathbf{x}, h)}}{Z}$$

- ◆ Graphical structure:

$$E(v, h) = -b'v - c'h - h'Wv$$



- ◆ Restrict the connectivity to make learning easier.

# Restricted Boltzmann Machines

- ◆ Factorized conditional distribution over hidden units

$$\begin{aligned} p(\mathbf{h} | \mathbf{v}) &= \frac{1}{p(\mathbf{v})} \frac{1}{Z} \exp \left\{ \mathbf{b}^\top \mathbf{v} + \mathbf{c}^\top \mathbf{h} + \mathbf{v}^\top \mathbf{W} \mathbf{h} \right\} \\ &= \frac{1}{Z'} \exp \left\{ \mathbf{c}^\top \mathbf{h} + \mathbf{v}^\top \mathbf{W} \mathbf{h} \right\} \\ &= \frac{1}{Z'} \exp \left\{ \sum_{j=1}^n c_j h_j + \sum_{j=1}^n \mathbf{v}^\top \mathbf{W}_{:,j} \mathbf{h}_j \right\} \\ &= \frac{1}{Z'} \prod_{j=1}^n \exp \left\{ c_j h_j + \mathbf{v}^\top \mathbf{W}_{:,j} \mathbf{h}_j \right\} \end{aligned}$$

# Restricted Boltzmann Machines

## ◆ For Gibbs sampling

- Hidden units:

$$\begin{aligned} P(h_j = 1 \mid \mathbf{v}) &= \frac{\tilde{P}(h_j = 1 \mid \mathbf{v})}{\tilde{P}(h_j = 0 \mid \mathbf{v}) + \tilde{P}(h_j = 1 \mid \mathbf{v})} \\ &= \frac{\exp \{c_j + \mathbf{v}^\top \mathbf{W}_{:,j}\}}{\exp \{0\} + \exp \{c_j + \mathbf{v}^\top \mathbf{W}_{:,j}\}} \\ &= \text{sigmoid} \left( c_j + \mathbf{v}^\top \mathbf{W}_{:,j} \right). \end{aligned}$$

- Observed units:

$$P(\mathbf{v} \mid \mathbf{h}) = \prod_{i=1}^d \text{sigmoid} (b_i + \mathbf{W}_{i,:} \mathbf{h})$$

# MLE

## ◆ Log-likelihood

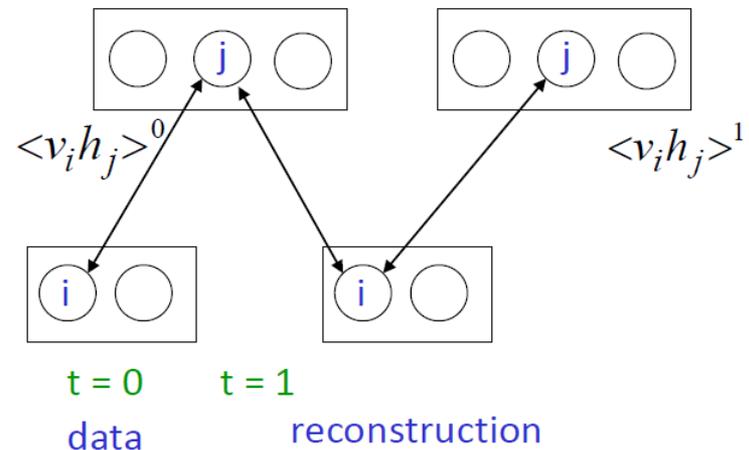
$$\begin{aligned} \ell(\mathbf{W}, \mathbf{b}, \mathbf{c}) &= \sum_{t=1}^n \log P(\mathbf{v}^{(t)}) \\ &= \sum_{t=1}^n \log \sum_{\mathbf{h}} \exp \left\{ -E(\mathbf{v}^{(t)}, \mathbf{h}) \right\} - n \log Z \end{aligned}$$

## ◆ Gradient

$$\begin{aligned} \frac{\partial}{\partial \boldsymbol{\theta}} \ell(\boldsymbol{\theta}) &= \frac{\partial}{\partial \boldsymbol{\theta}} \sum_{t=1}^n \log \sum_{\mathbf{h}} \exp \left\{ -E(\mathbf{v}^{(t)}, \mathbf{h}) \right\} - n \frac{\partial}{\partial \boldsymbol{\theta}} \log \sum_{\mathbf{v}, \mathbf{h}} \exp \left\{ -E(\mathbf{v}, \mathbf{h}) \right\} \\ &= \sum_{t=1}^n \frac{\sum_{\mathbf{h}} \exp \left\{ -E(\mathbf{v}^{(t)}, \mathbf{h}) \right\} \frac{\partial}{\partial \boldsymbol{\theta}} - E(\mathbf{v}^{(t)}, \mathbf{h})}{\sum_{\mathbf{h}} \exp \left\{ -E(\mathbf{v}^{(t)}, \mathbf{h}) \right\}} \\ &\quad - n \frac{\sum_{\mathbf{v}, \mathbf{h}} \exp \left\{ -E(\mathbf{v}, \mathbf{h}) \right\} \frac{\partial}{\partial \boldsymbol{\theta}} - E(\mathbf{v}, \mathbf{h})}{\sum_{\mathbf{v}, \mathbf{h}} \exp \left\{ -E(\mathbf{v}, \mathbf{h}) \right\}} \\ &= \sum_{t=1}^n \mathbb{E}_{P(\mathbf{h}|\mathbf{v}^{(t)})} \left[ \frac{\partial}{\partial \boldsymbol{\theta}} - E(\mathbf{v}^{(t)}, \mathbf{h}) \right] - n \mathbb{E}_{P(\mathbf{v}, \mathbf{h})} \left[ \frac{\partial}{\partial \boldsymbol{\theta}} - E(\mathbf{v}, \mathbf{h}) \right] \end{aligned}$$

# Contrastive Divergence (CD)

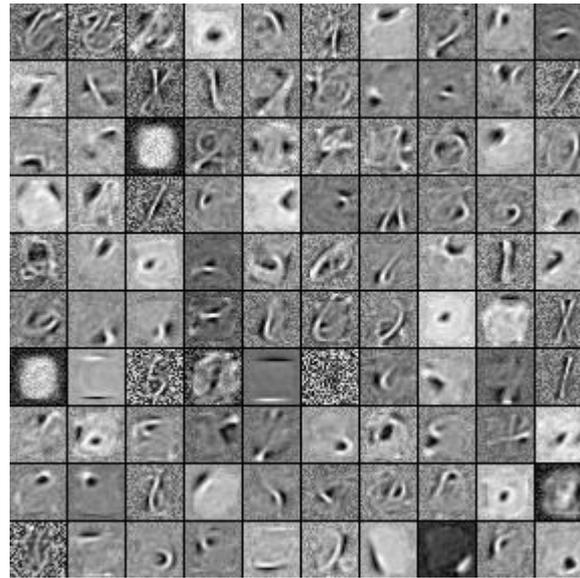
- ◆ Gibbs sampling for negative phase
  - Random initialization:  $v' \rightarrow h' \rightarrow \dots \rightarrow v \rightarrow h$
  - Slow because of long burn-in period
- ◆ Intuition of CD
  - Start from a data closed to the model samples
- ◆ CD-k for negative phase
  - Start from empirical data and run k-steps
  - Typically,  $k=1: v_1 \rightarrow h_1 \rightarrow v_2 \rightarrow h_2$



$$\Delta w_{ij} = \varepsilon (\langle v_i h_j \rangle^0 - \langle v_i h_j \rangle^1)$$

# RBM

◆ Filters



◆ Samples (RBM is a generative model)





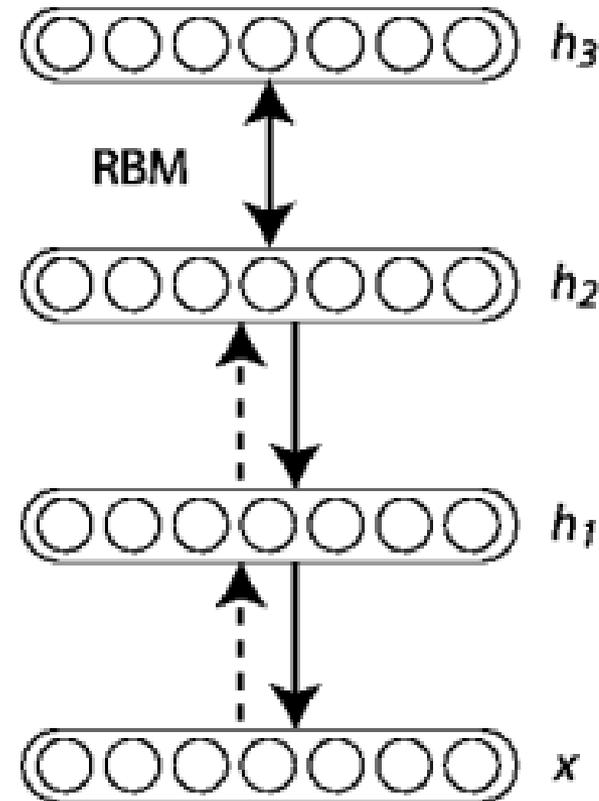
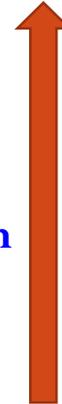
## Issues with RBM

- ◆ Log-partition function is intractable
- ◆ No direct metric for choosing hyper-parameters
- ◆ (one hidden layer) Much too simple for modeling high-dimensional and richly structured sensory data

# Deep Belief Nets – deep generative model

- ◆ [Hinton et al., 2006]
- ◆ Stacking RBM
- ◆ Greedy layerwise training
- ◆ Unsupervised learning
  - No labels
  - MLE

recognition



generation

# Neural Evidence?

- ◆ Our visual systems contain multilayer generative models
  
- ◆ Top-down connections:
  - Generate low-level features of images from high-level representations
  - Visual imagery, dreaming?
  
- ◆ Bottom-up connections:
  - Infer the high-level representations that would have generated an observed set of low-level features

# Recent Advances on DGMs

## ◆ Models:

- Deep belief networks (Salakhutdinov & Hinton, 2009)
- Autoregressive models (Larochelle & Murray, 2011; Gregor et al., 2014)
- Stochastic variations of neural networks (Bengio et al., 2014)
- ...

## ◆ Applications:

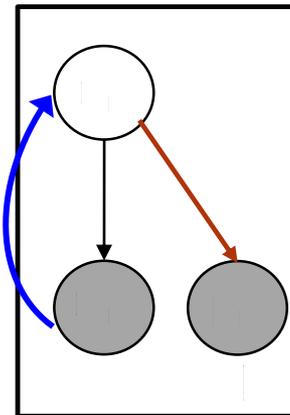
- Image recognition (Ranzato et al., 2011)
- Inference of hidden object parts (Lee et al., 2009)
- Semi-supervised learning (Kingma et al., 2014)
- Multimodal learning (Srivastava & Salakhutdinov, 2014; Karpathy et al., 2014)
- ...

## ◆ Learning algorithms

- Stochastic variational inference (Kingma & Welling, 2014; Rezende et al., 2014)
- ...

# Learning with a Recognition Model

- ◆ Characterize the variational distribution with a recognition model



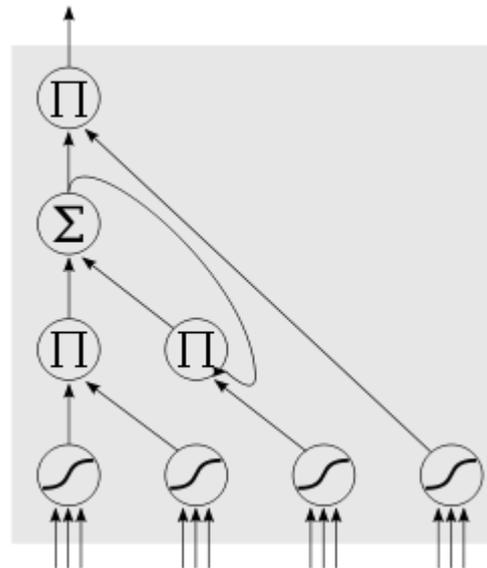
- ◆ For example:

$$q_{\phi}(\mathbf{z}|\mathbf{x}, y) = \mathcal{N}(\boldsymbol{\mu}(\mathbf{x}, y; \phi), \boldsymbol{\sigma}^2(\mathbf{x}, y; \phi))$$

- where both mean and variance are nonlinear function of data by a DNN

# Long Short-Term Memory

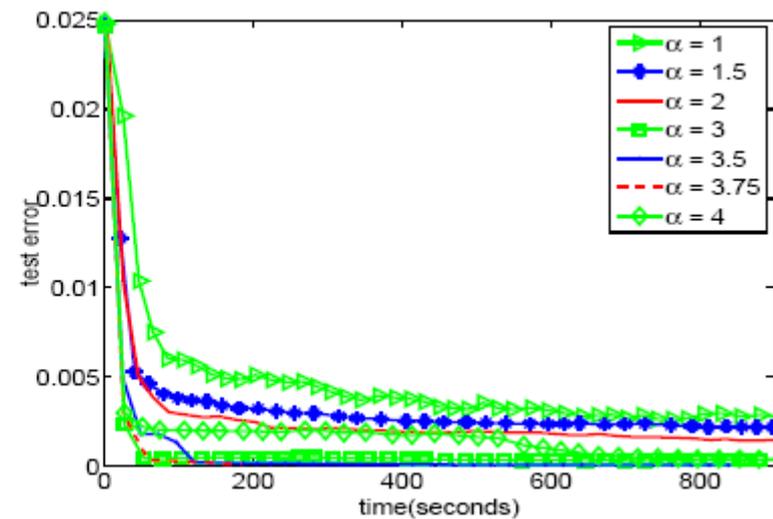
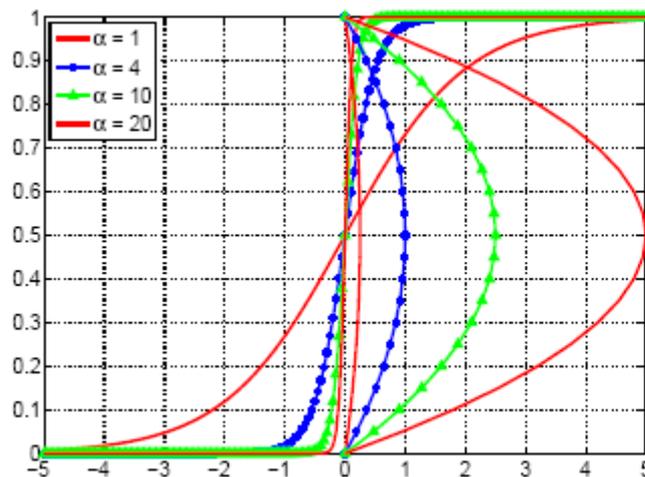
- ◆ A RNN architecture without gradient vanishing issue
- ◆ A RNN with LSTM blocks
  - Each block is a “smart” network, determining when to remember, when to continue to remember or forget, and when to output



# Issues

- ◆ The sharpness of Gates' activation functions matters!

$$f(x) = \frac{1}{1+e^{-\alpha*x}}$$





## Discussions



# Challenges of DL

## ◆ Learning

- Backpropagation is slow and prone to gradient vanishing
- Issues with non-convex optimization in high-dimensions

## ◆ Overfitting

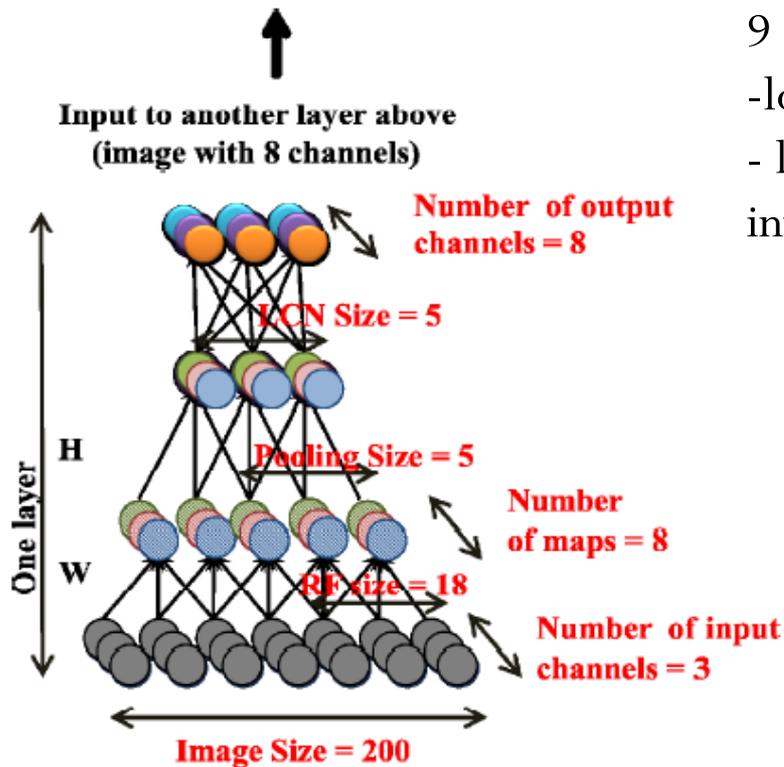
- Big models are lacking of statistical information to fit

## ◆ Interpretation

- Deep nets are often used as black-box tools for learning and inference

# Expensive to train

## ◆ “Big Model + Big Data + Big/Super Cluster”



9 layers sparse autoencoder with:

- local receptive fields to scale up;
- local L2 pooling and local contrast normalization for invariant features

- 1B parameters (connections)

- 10M 200x200 images

- train with 1K machines (16K cores) for 3 days

- able to build high-level concepts, e.g., cat faces and human bodies

- 15.8% accuracy in recognizing 22K objects (70% relative improvements)

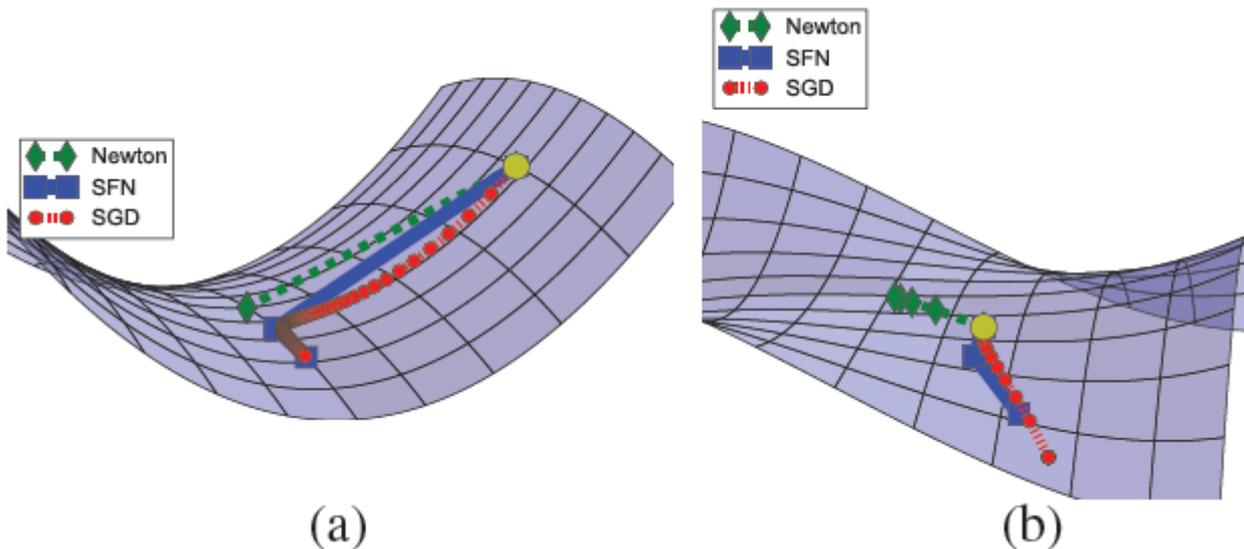


# Local Optima vs Saddle Points

- ◆ Statistic Physics provide analytical tools
- ◆ High-dimensional optimization problem
  - Most critical points are saddle points
  - The likelihood grows exponentially!

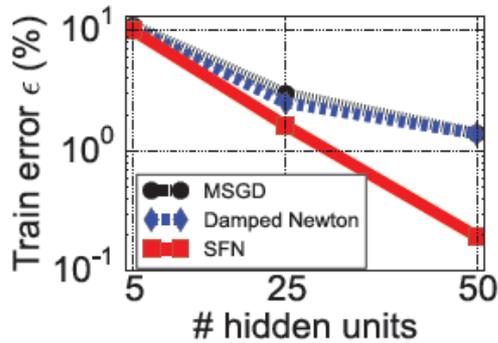
# Dynamics of Various Opt. Techniques

- ◆ SGD:
  - Gradient is accurate, but may suffer from slow steps
- ◆ Newton method:
  - Wrong directions when negative curvatures present
  - Saddle points become **attractors!** (can't escape)
- ◆ Saddle-free method:
  - A generalization of Newton's method to escape saddle points (**more rapidly than SGD**)

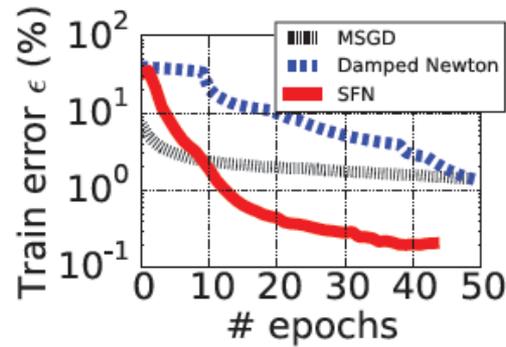


# Some Empirical Results

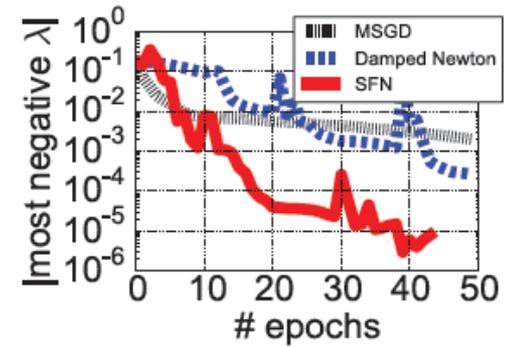
MNIST



(a)

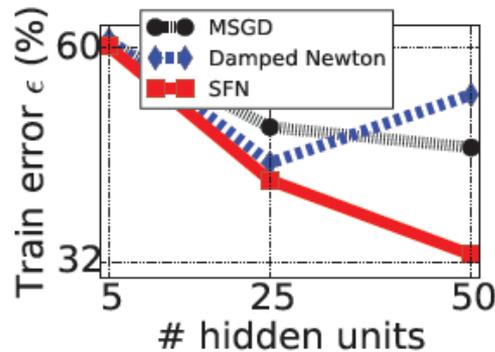


(b)

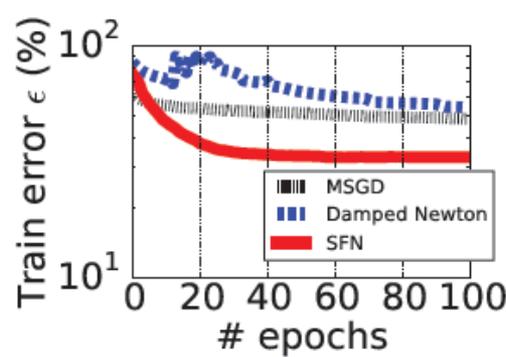


(c)

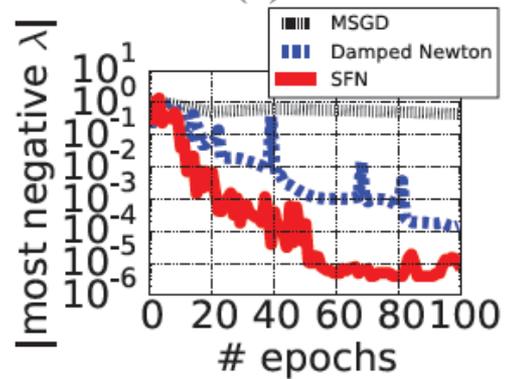
CIFAR-10



(d)



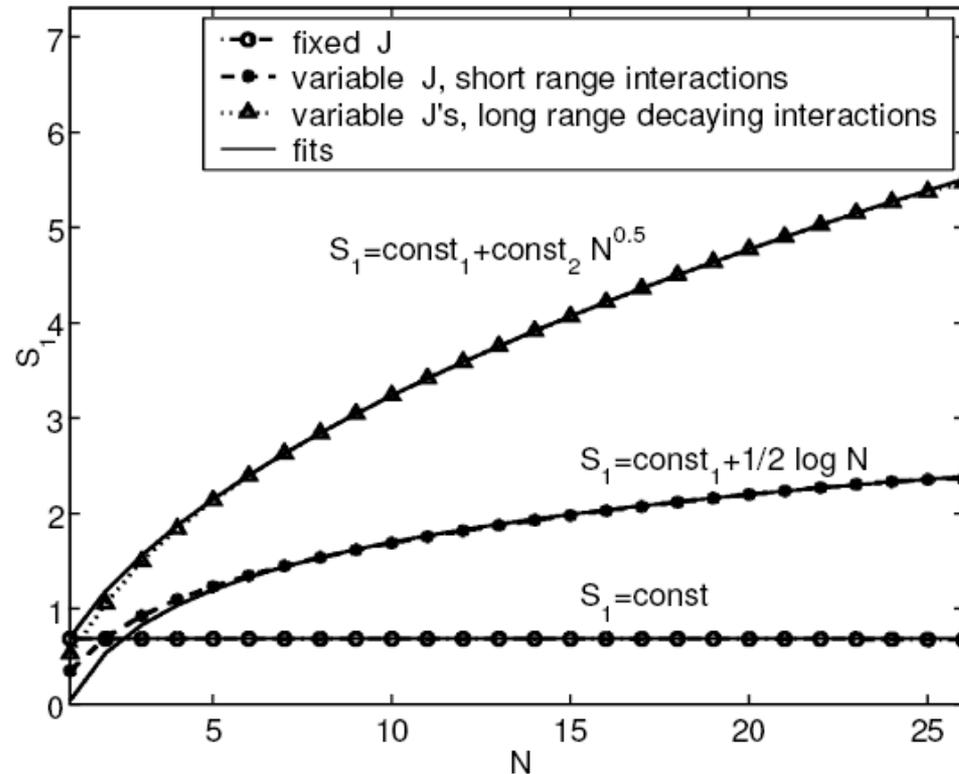
(e)



(f)

# Overfitting in Big Data

- ◆ **Predictive information** grows slower than the amount of Shannon entropy (Bialek et al., 2001)



# Overfitting in Big Data

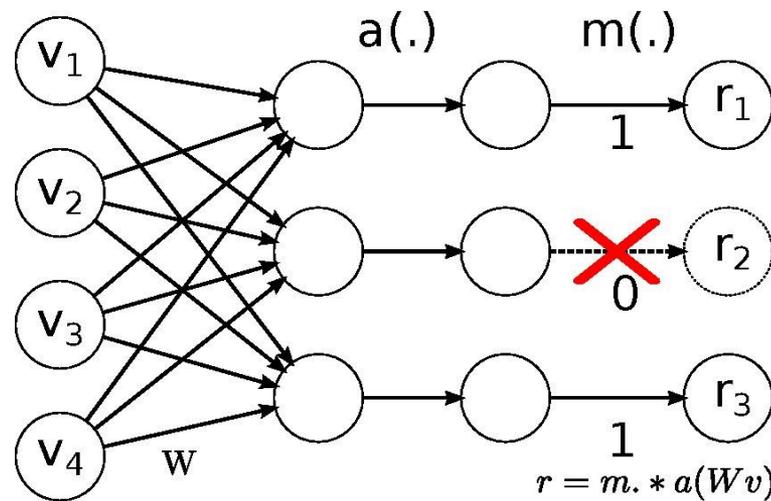
- ◆ **Predictive information** grows slower than the amount of Shannon entropy (Bialek et al., 2001)



**Model capacity grows faster than the amount of predictive information!**

# Overfitting in DL

- ◆ Increasing research attention, e.g., dropout training (Hinton, 2012)

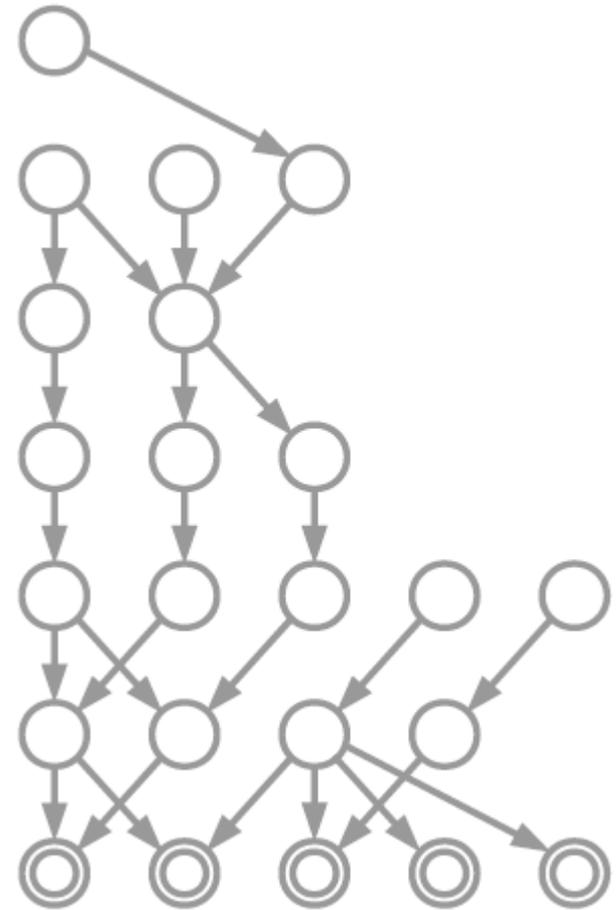


- ◆ More theoretical understanding and extensions
  - MCF (van der Maaten et al., 2013); Logistic-loss (Wager et al., 2013); Dropout SVM (Chen, Zhu et al., 2014)



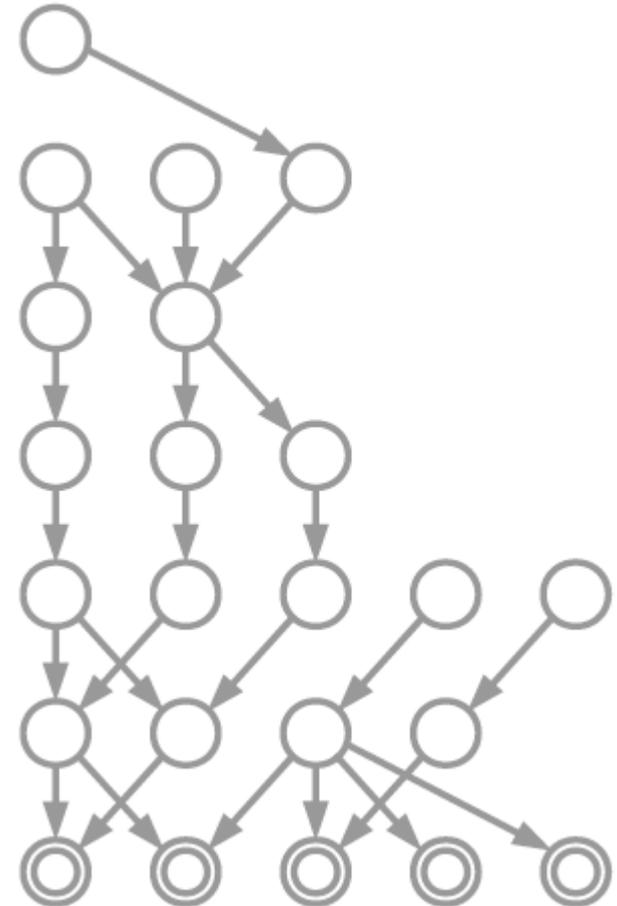
# Model Complexity

- ◆ What do we mean by structure learning in deep GMs?
  - # of layers
  - # of hidden units at each layer
  - The type of each hidden unit (discrete or continuous?)
  - The connection structures (i.e., edges) between hidden units
- ◆ Adams et al. presented a structure learning method using nonparametric Bayesian techniques – a cascading IBP (CIBP) process [Admas, Wallach & Ghahramani, 2010]



# Structure of Deep Belief Networks

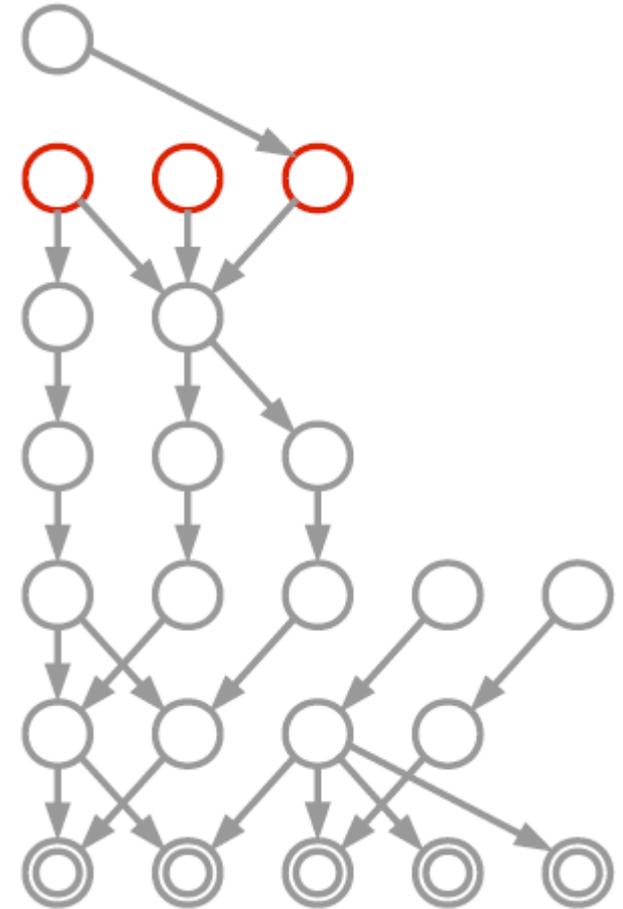
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[Animation by Wallach]

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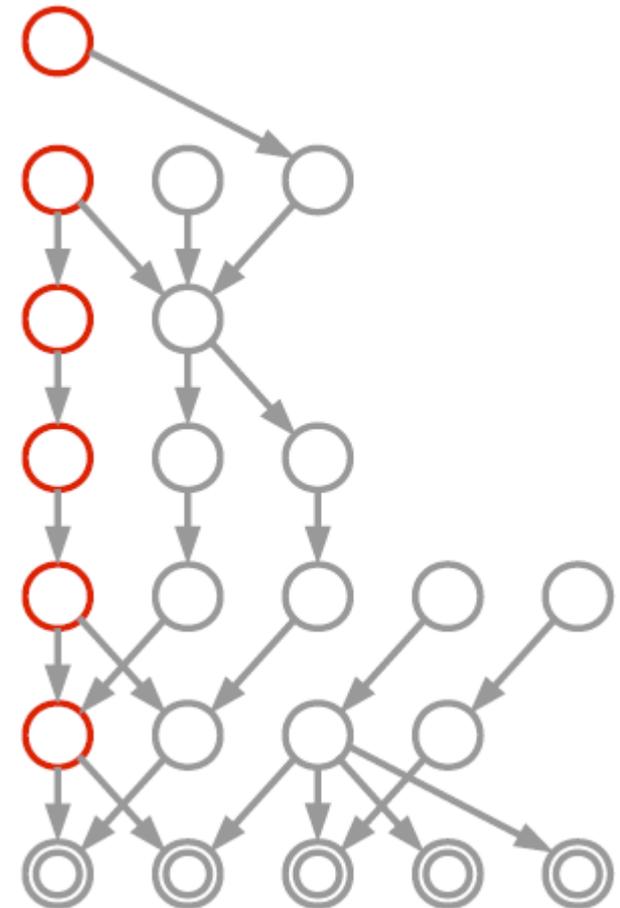
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[Animation by Wallach]

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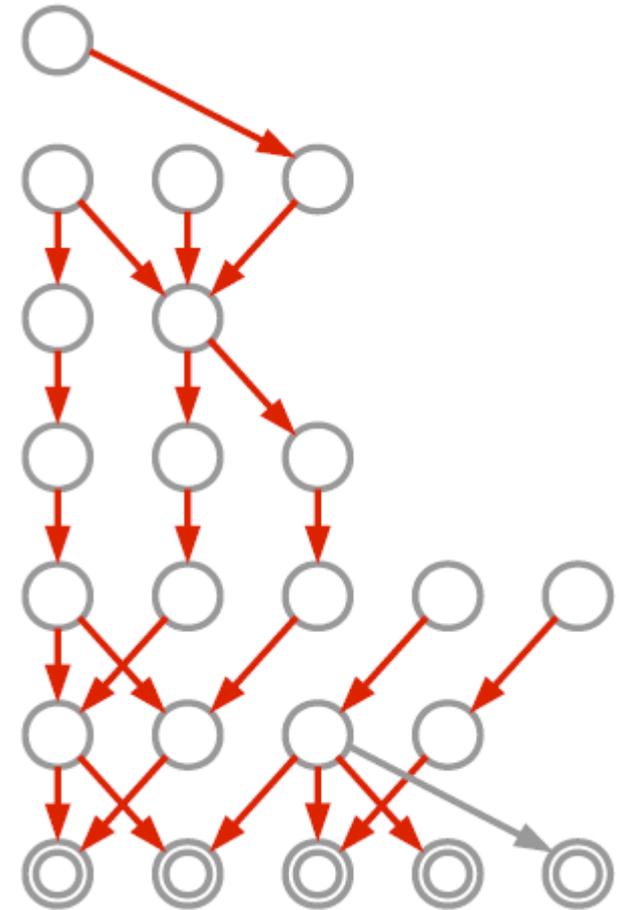
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[Animation by Wallach]

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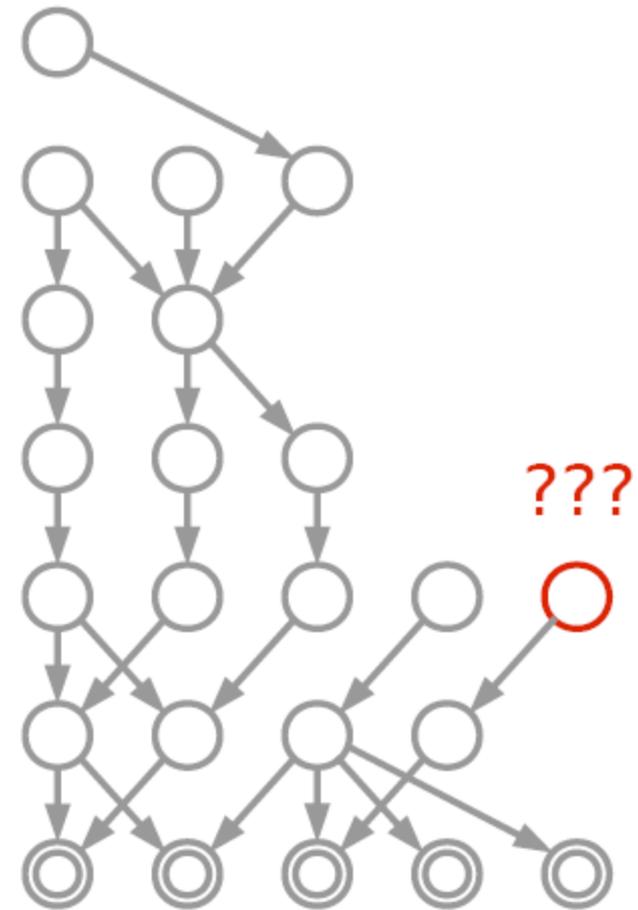
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[Animation by Wallach]

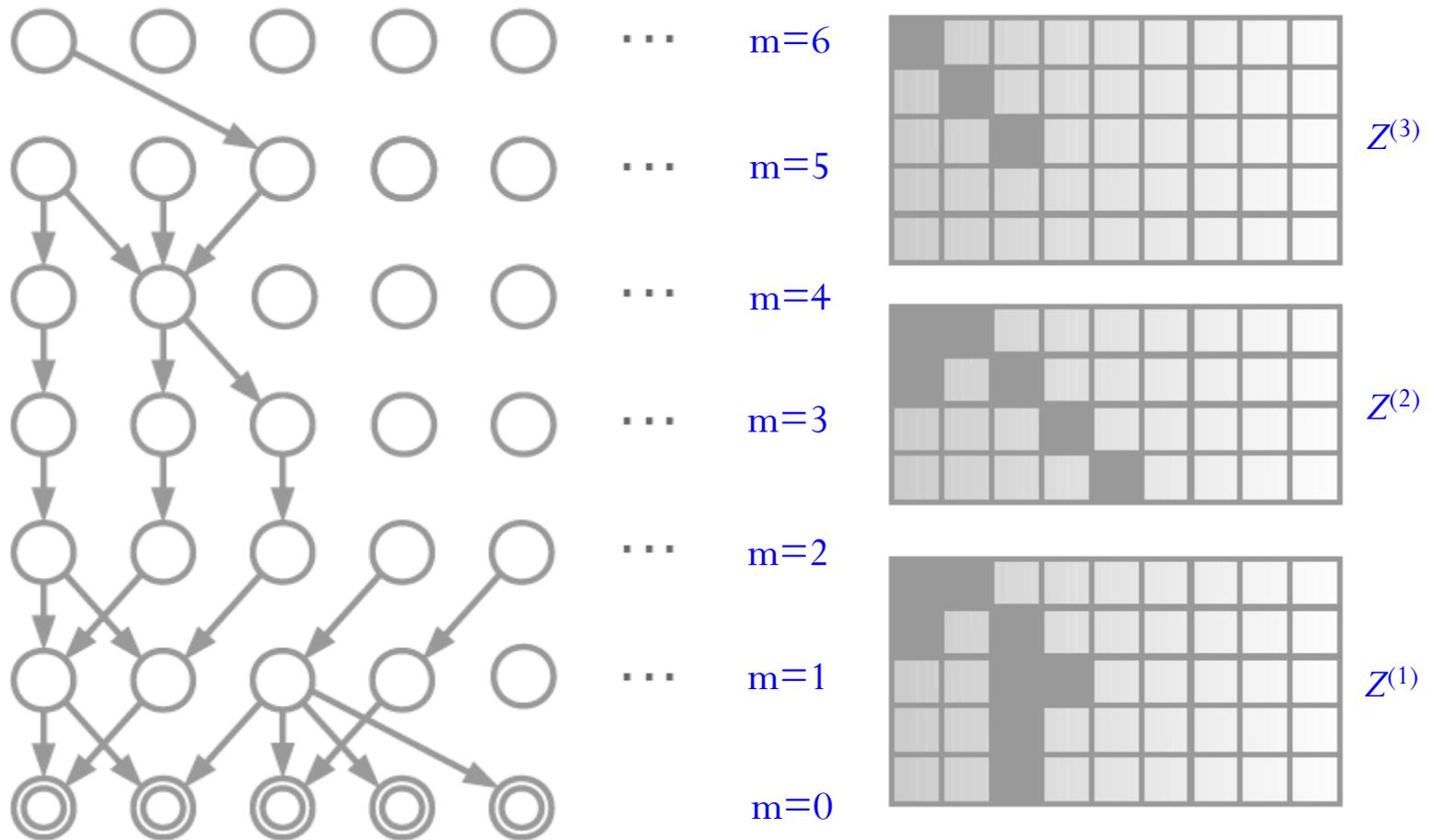
# Structure of Deep Belief Networks

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  - # of hidden units at each layer
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# Multi-Layer Belief Networks

◆ A sequence of binary matrices  $\Rightarrow$  deep BNs



# The Cascading IBP (CIBP)

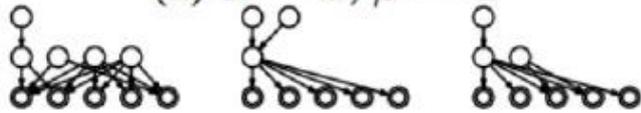
- ◆ A stochastic process which results in an infinite sequence of infinite binary matrices
  - Each matrix is exchangeable in both rows and columns
- ◆ How do we know the CIBP converges?
  - The number of dishes in one layer depends only on the number of customers in the previous layer
  - Can prove that this Markov chain reaches an absorbing state in finite time with probability one

# Samples from CIBP Prior

\* only connected units are shown



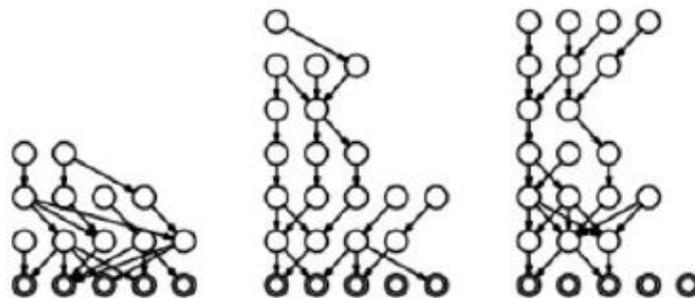
(a)  $\alpha = 1, \beta = 1$



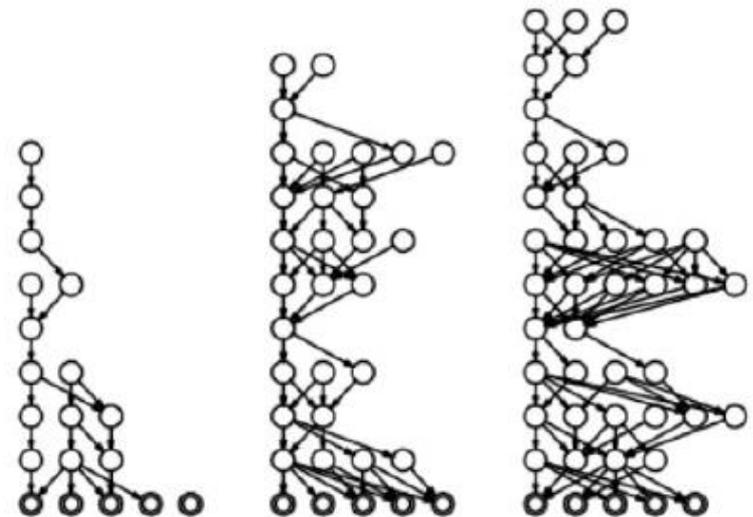
(b)  $\alpha = 1, \beta = \frac{1}{2}$



(c)  $\alpha = \frac{1}{2}, \beta = 1$



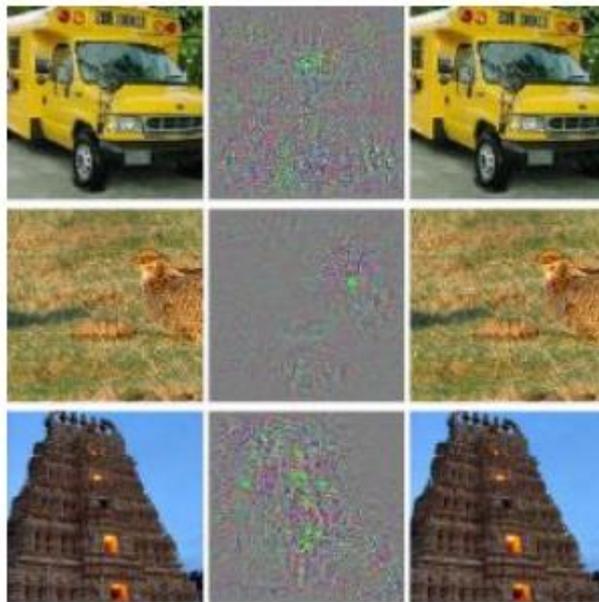
(d)  $\alpha = 1, \beta = 2$



(e)  $\alpha = \frac{3}{2}, \beta = 1$

# Some counter-intuitive properties

- ◆ Stability w.r.t small perturbations to inputs
  - Imperceptible non-random perturbation can arbitrarily change the prediction (**adversarial examples exist!**)



(a)

10x of  
differences



(b)



# Criticisms of DL

- ◆ Just a buzzword, or largely a rebranding of neural networks
  
- ◆ Lack of theory
  - gradient descent has been understood for a while
  - DL is often used as black-box
  
- ◆ DL is only part of the larger challenge of building intelligent machines, still lacking of:
  - causal relationships
  - logic inferences
  - integrating abstract knowledge



# How can neural science help?

- ◆ The current DL models:
  - loosely inspired by the densely interconnected neurons of the brain
  - mimic human learning by changing weights based on experience
  
- ◆ How to improve?
  - Transparent architecture?
    - Attention mechanism?
  
  - Cheap learning?
    - (partially) replace back-propagation?
  
  - Others?

# Will DL make other ML methods obsolete?

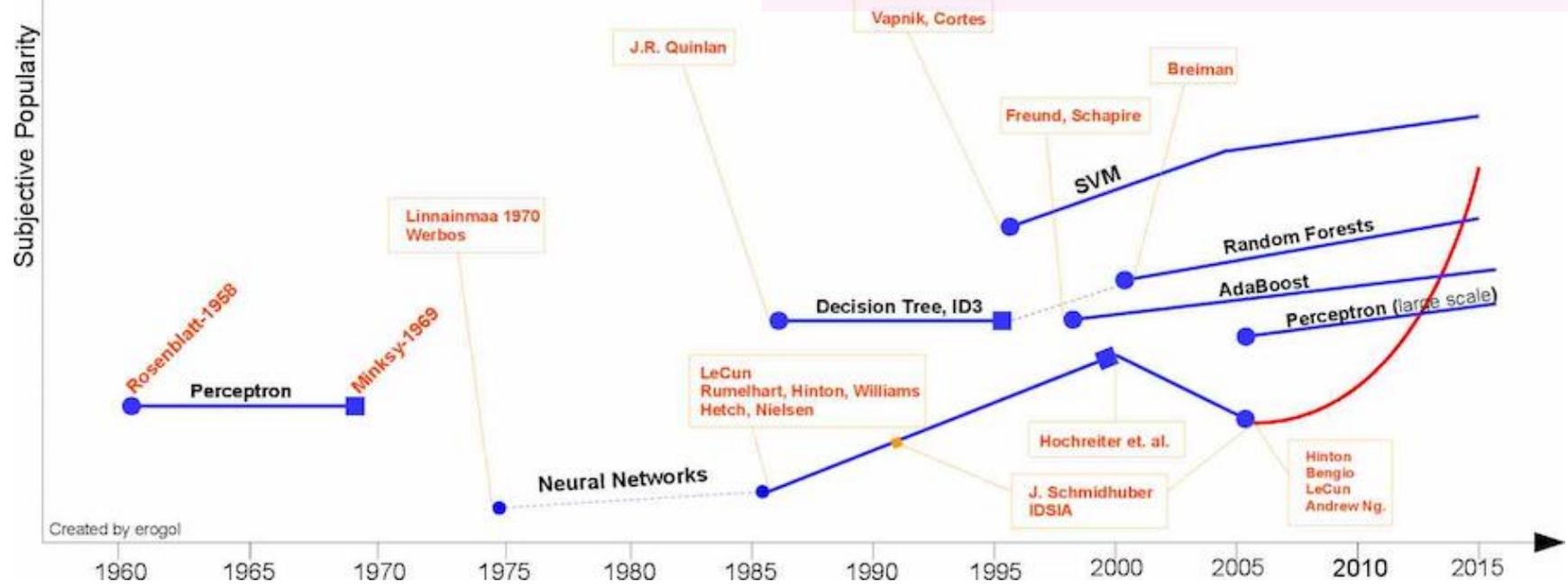
**Quora** 2014/12/23

**Yes** (2 post, 113 upvotes)

- best predictive power when data sufficient
- DL is far from saturated
- Google et al invests on DL, it is the “richest” AI topic

**No** (10 posts, 284 upvotes)

- simpler algorithms are just fine in many cases
- methods with domain knowledge works better
- DL is feature learning, needs other methods to work
- DL is not that well developed, a lot of work to be done using more traditional methods
- No free lunch
- a lot like how ANN was viewed in the late 80s



# What are people saying?

## ◆ Yann LeCun:

- “AI has gone from failure to failure, with bits of progress. This could be another leapfrog”

## ◆ Jitendra Malik:

- in the long term, deep learning may not win the day; ... “Over time people will decide what works best in different domains.”
- “Neural nets were always a delicate art to manage. There is some black magic involved”

## ◆ Andrew Ng:

- “Deep learning happens to have the property that if you feed it more data it gets better and better,”
- “Deep-learning algorithms aren't the only ones like that, but they're arguably the best — certainly the easiest. That's why it has huge promise for the future.”

# What are people saying?

## ◆ Oren Etzioni:

- “It’s like when we invented flight” (not using the brain for inspiration)

## ◆ Alternatives:

- Logic, knowledge base, grammars?
- Quantum AI/ML?



清华大学  
Tsinghua University

Thank You!